



UNSW
SYDNEY

FACULTY OF SCIENCE

**SCHOOL OF MATHEMATICS
AND STATISTICS**

INTRODUCTION TO MATLAB

2019

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Contents

1	What is MATLAB	2
1.1	What is MATLAB?	2
1.2	The MATLAB Window	3
1.3	Preparing MATLAB script Files	4
1.3.1	Using the MATLAB Editor	4
1.4	Online self-paced lessons for MATLAB	6
1.5	The MATLAB interface	7
1.5.1	Help facilities	7
2	MATLAB COMMANDS	9
2.1	Basics	9
2.1.1	Arithmetic	9
2.1.2	Assigning variables	9
2.1.3	Variable Names	10
2.1.4	Controlling Output	10
2.1.5	clear	11
2.1.6	Number Formats	11
2.1.7	Complex numbers	11
2.2	Saving Sessions, Input and Output	12
2.2.1	Data Input and Output	12
2.2.2	Recording your Session	12
2.3	Built-in Functions	13
2.4	Basic Vectors	13
2.4.1	Row and Column vectors	14
2.4.2	Vector arithmetic	14
2.4.3	Colon and linspace	15
2.5	Plotting	15
2.5.1	plot command	15
2.5.2	ezplot	16
2.5.3	Style options	16
2.5.4	Titles, axes and grids	17
2.5.5	Specialised plot procedures	17
2.6	M-files and New Functions	17
2.6.1	Function Files	18
2.6.2	Anonymous Functions	19
2.7	Further Vectors	20
2.7.1	Ordinary Product	20

2.7.2	Array Arithmetic	20
2.7.3	More on plotting	21
2.8	Matrices and Linear Equations	21
2.8.1	Definitions	21
2.8.2	Special matrices	22
2.8.3	Standard Matrix Arithmetic	23
2.8.4	Matrix array arithmetic	23
2.8.5	Systems of Linear Equations	23
2.9	Calculus	24
2.10	Programming Considerations	24
2.10.1	Logicals	24
2.10.2	If Statements	25
2.10.3	Loops	26
2.10.4	Other Control Structures	27

Chapter 1

What is MATLAB

1.1 What is MATLAB?

The MATLAB documentation describes MATLAB as a high-performance language for technical computing, integrating computation, visualisation, and programming in an easy-to-use environment where problems and solutions are expressed in familiar mathematical notation. Typical uses include

- Mathematics and computation;
- Algorithm development;
- Data acquisition;
- Modelling, simulation, and prototyping;
- Data analysis, exploration, and visualisation;
- Scientific, engineering and financial graphics;
- Application development, including graphical user interface building;

MATLAB is used for across a wide range of application areas covering science, engineering and business/finance.

MATLAB is an interactive system whose basic data element is an array that does not require dimensioning. This allows you to solve many technical computing problems, especially those with matrix and vector formulations, in a fraction of the time it would take to write a program in a scalar non-interactive language such as C or Fortran.

MAPLE, which is used in the standard first year mathematics courses, is an environment for doing mathematics. The basic object in MAPLE is an expression, which can be symbolically manipulated (for example integrated or differentiated). In contrast MATLAB is primarily a package for numerical computations whose basic object is a array. Both packages have integrated facilities for two and three dimensional visualisation and animation, tools which are essential for displaying and interpreting the results of mathematical models.

There are several versions of MATLAB. This chapter tells you how to use the version which is available in the School of Mathematics and Statistics' computer laboratories located on the ground floor and mezzanine level of the Red Centre. MATLAB is available on both the Linux and Windows computers in these laboratories. You may find other versions on computers elsewhere in the university and there is a student version [2] which you can buy from the UNSW Bookshop and run on your home computer. If you are UNSW students, you can download a free version of Matlab from UNSW IT website

<https://www.it.unsw.edu.au/students/software/matlab.html>.

You can also run Matlab on a mobile device using UNSW MyAccess service from <https://aaa-access.unsw.edu.au/vpn/index.html>.

Further information about MATLAB is contained in chapter 2, will be given in lectures, or will be in the reference books [4, 1]. The book [3] by Cleve Moler, one of the creators of MATLAB is available online, has an introduction to MATLAB and also to numerical methods. MATLAB has an extensive online help system.

In this chapter we will concentrate on the features of MATLAB common to both Linux and Windows and also on how to create the files needed for your course.

1.2 The MATLAB Window

To start a MATLAB **session** (i.e. open a MATLAB window), click on the MATLAB Application Icon:

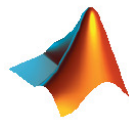


Figure 1.1: MATLAB icon

After some time, a MATLAB window, similar to that shown in figure 1.2, will appear.

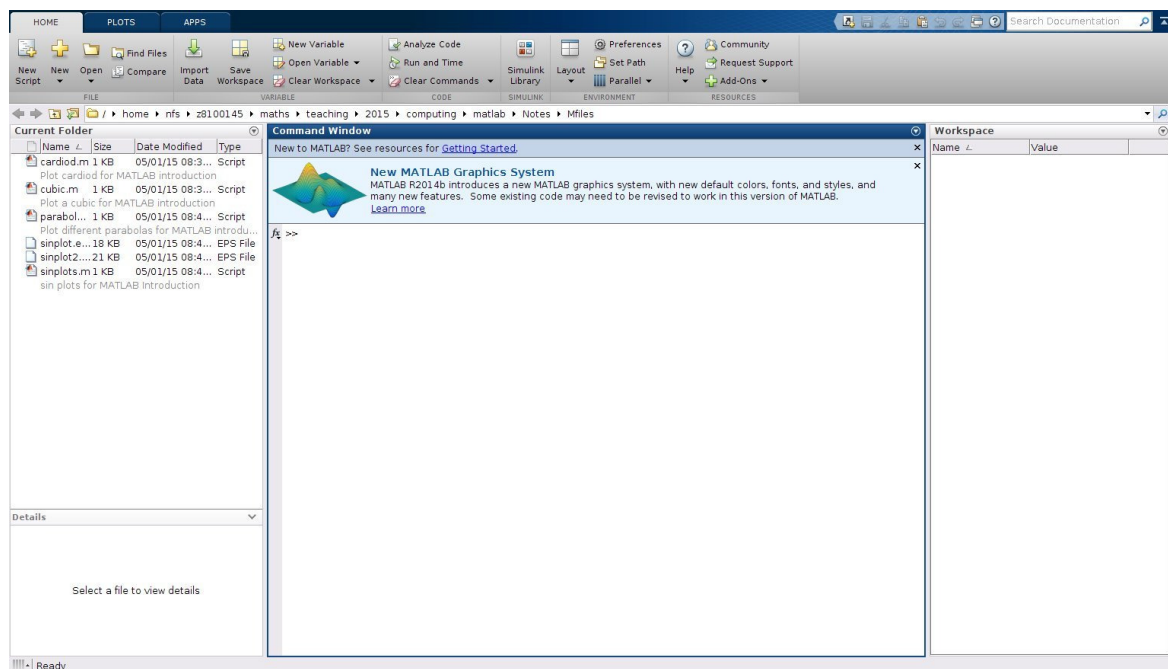


Figure 1.2: Initial MATLAB windows

Figure 1.2 shows the MATLAB windows when you start MATLAB for the first time. This window contains a tabbed set of menus across the top and a Search Documentation box in the top right hand corner. Most of the time you will be using the HOME tab. Immediately below the menu tab is a list of the folders you are in, ending in MATLAB's

4 CHAPTER 1. WHAT IS MATLAB

current folder. It is good practice to create folders for your different courses, all under your UNSW home drive (not on the local computer) so you can access them from any computer.

The first time you start MATLAB the main window will be split into several sub-windows, including the **Current Folder**, **Command Window**, **Workspace** and **Command History**.

- The **Current Folder** sub-window lists all the files in the the current folder.
- The **Command Window** is where you type commands and see the results of commands that MATLAB has executed. The **Command Window** has the MATLAB prompt `>>`, indicating MATLAB is waiting for you to enter a command.
- The **Workspace** sub-window lists the variables you have created and some of their properties.
- The **Command History** sub-window lists the commands you have used recently, enabling you to easily go back to a previous command.

After you have become familiar with MATLAB, all but the main **Command** window may be closed. This depends on what you find to be the most efficient way to work. You may also like to change the height and width of this window as well.

Note: *Throughout this chapter (unless otherwise stated) we will use ‘click’ to mean ‘click the left mouse button’.*

When you want to terminate a MATLAB session (i.e. close a MATLAB window), either simply type `quit` at the MATLAB prompt, or click the close button (small circle with a x) in the top right hand corner. When you quit MATLAB your configuration is saved. The next time you start MATLAB, your saved configuration will be used.

1.3 Preparing MATLAB script Files

You will prepare **script files** and **function files** during laboratory classes. These are both often called **M-files**, as they all have the file extension `.m` (lower case). A script file contains commands to carry out specified tasks; a function file defines a MATLAB function. These files are discussed in more detail in section 2.6, and will be covered in lectures. Both types of file should also contain comments — these could give the purpose of the M-file, how to use a function M-file or particular features of your code.

NOTE that a MATLAB M-file is a text file which contains *nothing except a list of MATLAB commands* (with no prompts) and comments (which start with a `%`).

You should first read the relevant parts of the lecture notes, these notes, any reference book and work out a suitable sequence of commands. Then you should try them out on the computer and modify them if they do not work. Finally you save the script file for later reference.

1.3.1 Using the MATLAB Editor

An editor is a piece of software used for editing files (also known as word-processing). Since M-files are text files, any editor can be used.

However, MATLAB has its own built in editor which has the advantage of being purpose built for creating script and function files. Among its features, the MATLAB editor has

- **Syntax highlighting:** for example, comments (green) and strings (purple) appear in different colours to commands.

- **Program layout:** easily indent your MATLAB code to reflect the program structure.
- **Debugging support:** breakpoints may be set on any executable line of a M-file and the values of any quantities inspected and manipulated.
- **Profiling:** collect information on the amount of CPU time taken by functions and individual lines of code.

To start the MATLAB Editor, click the **New Script** icon (this is the first of the icons in the icon bar in Figure 1.2) or type the command `edit` in the command window. A new window appears: the MATLAB Editor. Alternatively you can use the **Open** icon to open an existing file, or type the command `edit cubic.m`. If the file `cubic.m` is not in MATLAB's current folder then MATLAB will ask you if you want to create the file. Figure 1.3 shows a MATLAB Editor window, with a script file called `cubic.m` that will

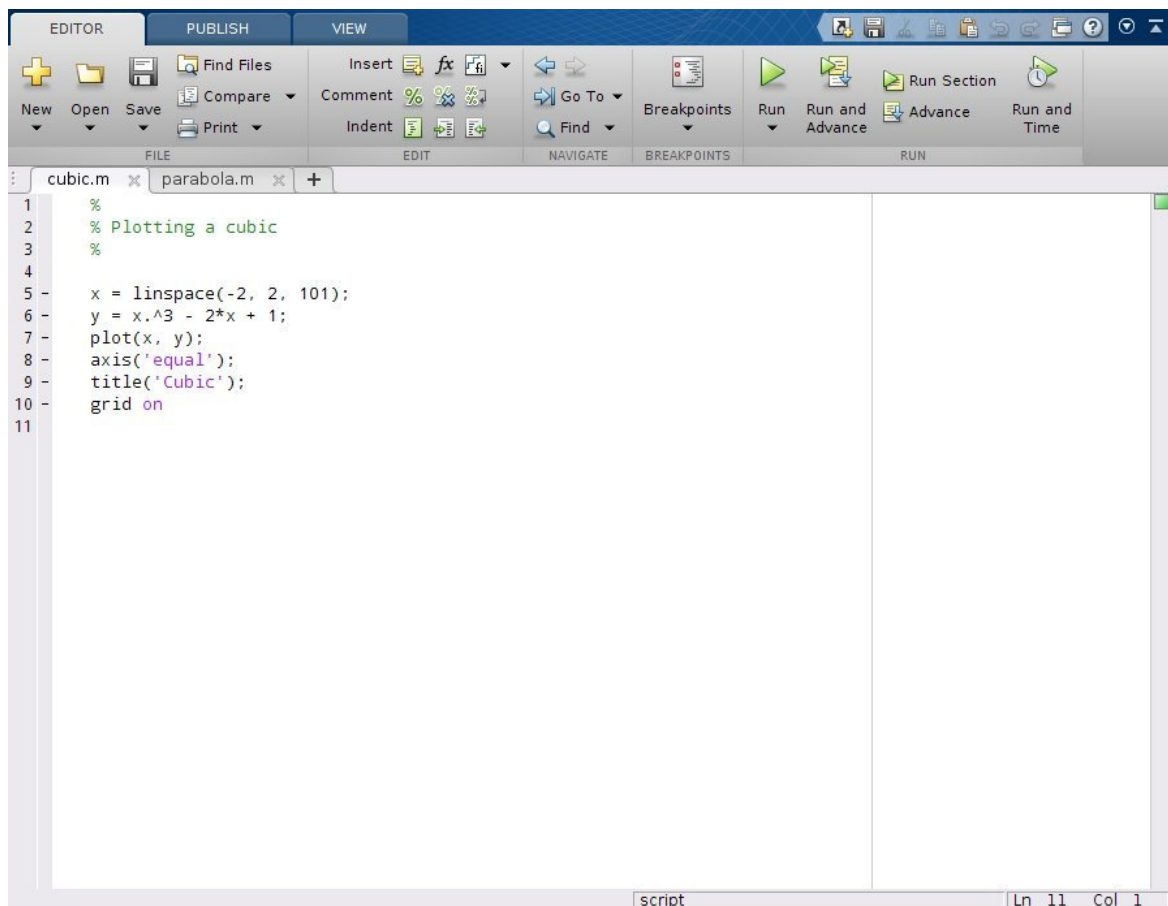


Figure 1.3: A MATLAB Editor Window

draw a cubic when executed. The MATLAB editor window has its own menus and tabs with icons. These behave in roughly the same way as the corresponding icons in, for example, Microsoft Word. Note that clicking on the first of the icons will open up a new **buffer** (editing space), so it is possible to have several M-files being edited at the same time. Just under the tabs with the various icons is a list of **tabs** with the names of the M-files being edited: click on the appropriate name to change to that file. You may see that there is a second file called `parabola.m` being edited in figure 1.3.

6 CHAPTER 1. WHAT IS MATLAB

Before you can run an M-file, that is sequentially execute all the MATLAB commands in the file, you must save the file **and** the file must be in MATLAB's current folder. Check the files is listed in the **Current Folder** sub-window (see Figure 1.2), or type the command **what** in the command window. A very common mistake is to edit and save a file which is not in MATLAB's current folder, so it cannot be run.

Note that the lines beginning with a % sign are **comments**. MATLAB ignores everything on a line that comes after a % sign.

When saving a script file, you will have to give the file a suitable name; with function files the editor will fill in the name for you — it will always be the name of the function (with the **.m** file extension added).

To prepare a MATLAB M-file using a different editor, you work out what commands you want to use and simply use the editor to create a text file containing these commands (and suitable comments).

Don't forget to check that

- irrelevant output is suppressed by ending appropriate commands with a semicolon
- your file works

To check that your script file works enter the MATLAB command **clear** to clear all variables in the current workspace (see section 2.1.5 for more information on the **clear** command). Then enter the name of the file (without the **.m**) and the file should run.

To check that a function file works just use the function as if it were a standard MATLAB function (without any **.m** extension).

Note: We advise you *always* to do these checks; the commonest problems are caused by students creating an M-file that *does not work*. Running this check will enable you to spot where errors occur and save a great deal of time, frustration and marks.

Exercise Open a MATLAB session and open the MATLAB editor. Enter the commands in figure 1.3 and save the file as **cubic.m**.

Then activate the MATLAB command window and enter **cubic** at the MATLAB prompt and press the **Enter** key. Running the file **cubic.m** should produce a plot of the cubic in a new window.

When you press the **Enter** key, MATLAB immediately tries to interpret and execute the command(s) you have entered. If the command is the name of a script M-file, then MATLAB will try to sequentially interpret and execute all the commands in the file.

1.4 Online self-paced lessons for MATLAB

A number of introductory self-paced learning modules to provide an introduction to MATLAB are available through your course on the Moodle Learning Management System. You should work through these, preferably at a computer with MATLAB running so you can try all the exercises. You can also use these notes as an additional reference. The on-line MATLAB learning modules also include tests using Maple TA, which may count as part of the assessment for your course.

You are expected to create and store in a logical fashion script or function M-files that answer exercises. These may be inspected as part of the assessment of your laboratory participation mark or you may be required to create M-files as part of your MATLAB computer laboratory test.

1.5 The MATLAB interface

The MATLAB tabbed interface, both for the main MATLAB window and the MATLAB editor has a large number of icons and associated menus. This tabbed interface was introduced in MATLAB R2012b, so older versions have a (very) different graphical user interface (GUI). The underlying MATLAB commands are still the same.

A context sensitive set of menus (that is it changes depending on which window/sub-window is active) can be obtained by right-clicking. This is often the most efficient way of accomplishing a task. For example if you have a complicated script open in the editor with various structural elements, then using the right-click and choosing **Select All** followed by **Smart Indent** causes MATLAB to automatically indent loops and logical blocks.

Note that in the MATLAB editor, roughly in the middle of the **HOME** tab, is a large green arrow labelled **Run** (see Figure 1.3). Clicking this arrow gets MATLAB to first save the current file that is being edited and then to try to run the file. Any syntax errors are reported in the command window, coloured in red. There will also be a link to the line in the file which caused the error. Clicking on this link will open the file in the MATLAB editor and position the mouse as close to the source of the error as possible.

Warning: The School of Mathematics and Statistics holds computer laboratory exams in many courses. For these exams the computers are in a special Linux based exam mode. While MATLAB runs on Windows, Linux and Macintosh operating systems, the short-cut control keys are often different between the different operating systems. For example in the Windows version of the MATLAB editor, Cut and Paste are Ctrl+c and Ctrl+v respectively, while under Linux Cut and Paste are Alt+w and Ctrl+y respectively. Thus it is preferable not to depend heavily on the use of short-cut keys. The context sensitive menu obtained by right-clicking gives you the same set of items under both Windows and Linux.

1.5.1 Help facilities

MATLAB comes with a variety of help facilities as part of the software product (plus many more available over the www). A MATLAB command in the file `task.m` uses the comments (up to the first blank line) at the beginning of the file or function to provide documentation about the purpose of the script and input and output arguments for functions.

In the MATLAB command window, typing

```
help exp
```

displays information in the command sub-window about the `exp` function which is obtained from the comments at the beginning of the file `exp.m`. At the bottom of the information displayed in the command window are suggestions for related commands (for example the `log` command with `help exp`. (Do not worry if you have not heard of some of these commands at this stage).

MATLAB's help browser, pictured in figure 1.4, provides another interface to MATLAB's documentation.. The information from the comments at the beginning of a file may be displayed in MATLAB's help browser using the links at the end of the information displayed by the `help` command, or directly with the command

```
doc exp
```

8 CHAPTER 1. WHAT IS MATLAB

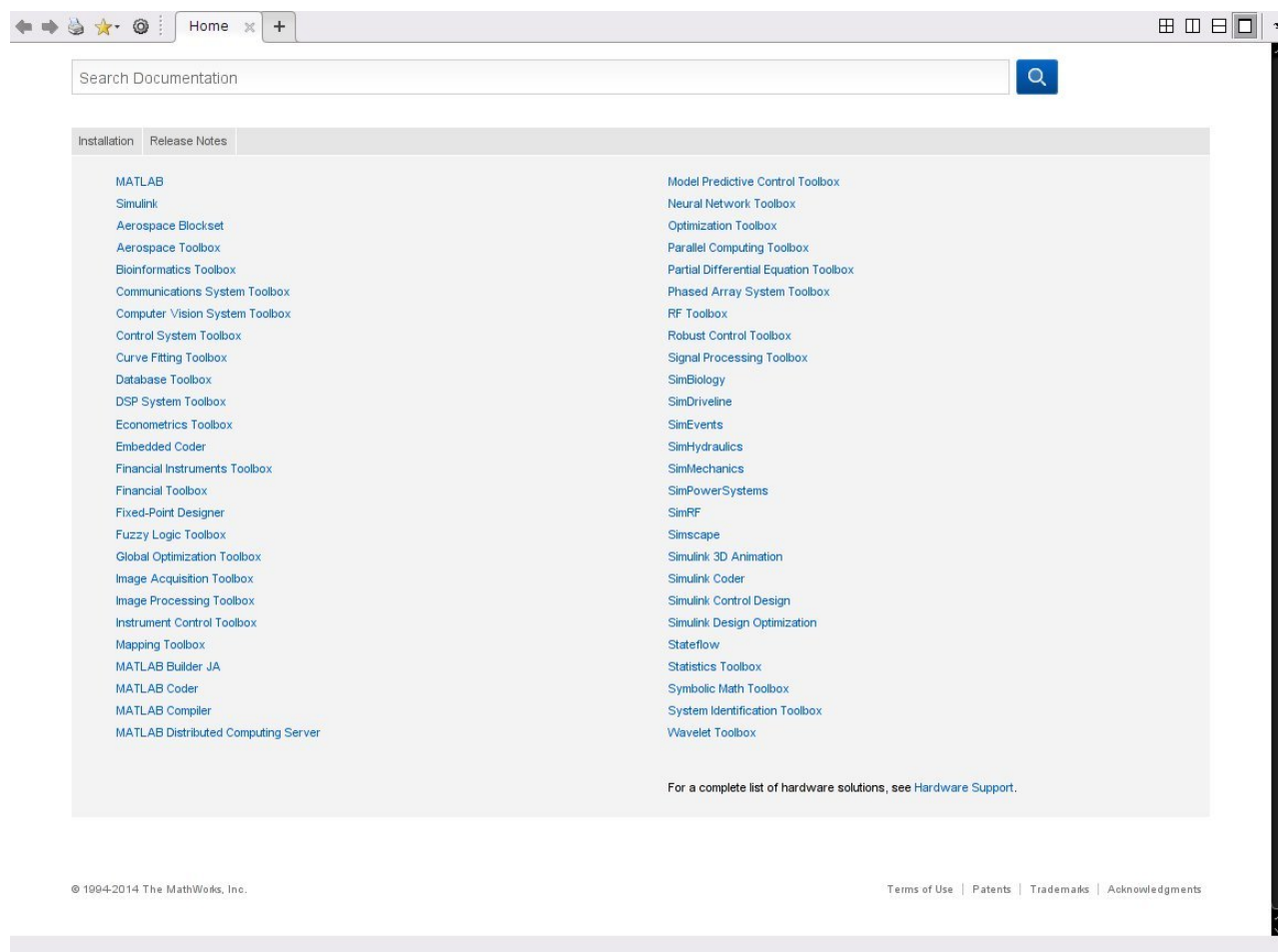


Figure 1.4: The Help browser window with a listing of available toolboxes

You can also search for information using the **Search Documentation** box in the top right hand corner of the main MATLAB window – see Figure 1.2 or MATLAB editor – see Figure 1.3. Alternatively MATLAB’s help browser can be opened by clicking on the question mark ? in a small circle just to the left of the **Search Documentation** box. You can then enter the term you wish to search for. You can search the help pages either for a known function name or search for a phrase if you do not know the command name (for example, search on “log”).

The documentation for both **exp** and **log** mentions complex numbers which you may have seen in high school mathematics, but will definitely see in first year university mathematics. One of the powers of packages like MATLAB, in contrast to Microsoft Excel for example, is that MATLAB can automatically work with complex numbers (this is both powerful and dangerous).

The best way to learn how to use MATLAB is to experiment and try commands, and explore the online help facilities and examples. The Help browser has tutorials and information about MATLAB **toolboxes** (additional packages of programs for special applications – see Figure 1.4) amongst other information. You may use the Help browser in the laboratory. It may also be used in MATLAB tests held in the computer laboratory.

Chapter 2

MATLAB COMMANDS

This chapter provides an introduction to some MATLAB commands and basic features of the language. More details will be provided during your course. There are many books on MATLAB and its use in Engineering, Science and Business. Cleve Moler, one of the founders of MATLAB, has a text book [3], while the MATLAB Guide [1] is very useful for more advanced techniques.

The best way to use this chapter is first to glance through it to get an idea of what MATLAB can do (actually it can do far more than what we have described here), bearing in mind that many of the things in this chapter refer to mathematical ideas and processes covered in first year mathematics courses. Later, when you are solving a specific problem, read through the relevant sections of this chapter and your lecture notes, before preparing a list of MATLAB commands to solve that problem. Then, when you are entering these commands, use MATLAB's Help browser (see section 1.5.1) for the exact syntax.

NOTE There are built in demos in MATLAB. To use them, either enter the command
`demo`

during a MATLAB session or select the "Demos" tab in the MATLAB Help browser window. For further information, see section 1.5.1.

2.1 Basics

2.1.1 Arithmetic

The usual arithmetic operations are available in MATLAB and you should use the following notation to enter them in commands.

addition	+
subtraction	-
multiplication	*
division	/
exponentiation	^

So a^b means a to the power b (i.e. a^b).

These follow the usual order of evaluation, i.e. anything in brackets, then powers, then multiplication or division, then addition or subtraction.

If you want to use a different order then you will have to insert brackets '(' and ')' in the appropriate places. For example $-1^{(1/2)}$ means $-(1^{(1/2)})$ (i.e. -1), whereas $(-1)^{(1/2)}$ means $\sqrt{-1}$ (i.e. the imaginary number i , which is denoted `1.0000i` in MATLAB) and $-1^{1/2}$ gives -0.5000 .

2.1.2 Assigning variables

You use `=` to assign a value to a variable, for example

```
x=1,f = sin(x)
```

10 CHAPTER 2. MATLAB COMMANDS

This assigns the value 1 to x and then $\sin(1) \approx 0.8415$ to the variable f . If x were an unknown (it had not been assigned a value), then you would get an error message.

What we have been doing is called **assigning a value to a variable** and the general format for doing it is

variable_name = expression

After you have given an assignment command, MATLAB will replace the named variable with its assigned value wherever that variable name occurs in the future.

If you do not assign an answer to a variable, then MATLAB will assign the result of the calculation to the default variable **ans**, which you can then use in the next calculation like any other assigned variable.

2.1.3 Variable Names

Variable names must start with a letter and the initial letter can be followed by letters, digits and the underline character “_”.

There is effectively no limit to the length of a name, but MATLAB only looks at the first few characters, where “few” depends on how that system is set up: on the version in the Mathematics and Statistics computer laboratories it is the first 63 characters that count (see the command **namelengthmax**). Upper and lower case letters are treated as *different* in names. Here are some examples

t t3 A_b T time

You should avoid using names already used as function names for your own variables, as then you would be unable to use the function. You can test to see if a name is being used by a command like

```
>> which -all tan_x
tan_x not found.
```

This means that **tan_x** can be used as a variable. Anything else means it cannot.

Special Variables

Five names stand for constants that are important namely,

pi	$\pi \approx 3.14159265358979$
i or j	$i = \sqrt{-1}$
Inf	∞
eps	$2^{-52} \approx 2.2 \times 10^{-16}$ the machine epsilon

The machine epsilon **eps** is the smallest positive number such that MATLAB considers $1+\text{eps}$ to be greater than 1.

2.1.4 Controlling Output

Often in doing MATLAB calculations you will create a very long output that you do not need to actually see. You should get into the habit of **suppressing** long output by ending such commands with a semi-colon ; so that your MATLAB screen does not get cluttered up. So for example

```
>> a=3; b=5^2-a^2
b =
    16
```

You can also control the amount of space that MATLAB uses between lines using the command **format compact**.

2.1.5 clear

The command `clear` can be used to remove variables and functions from memory:

```
clear           clears all variables
clear functions clears (i.e. forgets about) all M-files and other defined functions
clear a b      clears variables (or M-files) a and b only
clear all      clears everything: variables, M-files etc.
```

See the help on `clear` for further detail.

2.1.6 Number Formats

MATLAB does all its calculations in IEEE double precision (64 bit) floating point binary arithmetic. This means that MATLAB works to about 16 decimal digits and can handle floating point numbers as large as about 10^{308} and as small as about 10^{-308} . See the functions `realmin` and `realmax`.

To control how a number is displayed, you use the `format` command: changing the format has no effect on MATLAB's internal calculations.

The following table shows the output of $\sqrt{2009}$ in the various formats.

command	output	
<code>format short</code>	44.8219	this is the default
<code>format short e</code>	4.4822e+01	that is, 4.4833×10^1 , note rounding
<code>format long</code>	44.821869662029940	16 places (double precision)
<code>format long e</code>	4.482186966202994e+01	
<code>format bank</code>	44.82	as if it were money
<code>format rat</code>	14343/320	a rational approximation

There are two other possible types of output you might get from MATLAB:

Result	Meaning
Inf	∞
NaN	not a number, e.g. 0/0

2.1.7 Complex numbers

MATLAB can also handle complex numbers, such as $i = \sqrt{-1}$. MATLAB will recognise both `i` and `j` (if they have not been used as variable names) as this complex number. For example

```
>> 1/2+sqrt(3)*i/2
ans =
    0.5000 + 0.8660i
```

The commands `real`, `imag`, `abs` and `angle` when applied to a complex number give, respectively, the real part, imaginary part, modulus (absolute value) and argument of the complex number. For example:

```
>> z=1/2-3*i/4;
>> real(z),imag(z),abs(z),angle(z)
ans =
```

12 CHAPTER 2. MATLAB COMMANDS

```
    0.5000
ans =
   -0.7500
ans =
    0.9014
ans =
   -0.9828
```

You could also have defined the complex number z by `z = complex(1/2,-3/4)`

2.2 Saving Sessions, Input and Output

MATLAB's main purpose is to perform tasks on large amounts of data, so you need to be able to get data into MATLAB and save data from MATLAB for later processing. In some of the laboratories exercises, you may be asked to perform some analysis on data will be provided for you (such as the temperature at each point of a grid in a two or three dimensional object or daily share prices for a portfolio of fifty stocks over two years). It is also useful to be able to record your MATLAB session so that you can later rerun the same commands, maybe with different data or with minor modifications.

2.2.1 Data Input and Output

The `save` command is used to save the values of some or all of the variables in your MATLAB session. This command saves into a file known as a **Mat-file**. Note that you cannot edit these files, as the information is stored in a binary (non ASCII) format. Also, Mat-files must have the `.mat` file extension, which MATLAB will add if you do not.

The `load` command does the opposite of `save`, and loads a Mat-file into the workspace. For example,

```
>> save price.mat jan feb
>> save apr21
>> load apr1
```


The first command saves variables `jan` and `feb` to the file `price.mat`; the second saves all variables into the file `apr21.mat`, with the `.mat` automatically added by MATLAB; the last command loads the file `apr1.mat`, again automatically adding the `.mat` extension.

2.2.2 Recording your Session

MATLAB has a built in feature that allows you to re-run the previous commands: a **history** file. This file stores all the previous commands you have entered into MATLAB as you type them. You can see this in the the **Command History** sub-window (see Figure 1.2).

If you are using more than a couple of commands it is better to write a script file (see section 2.6) when you use MATLAB.

If the **Command History** sub-window is not displayed, tick the box “Command History” under the **Layout** icon. If you double click on a command in **Command History** sub-window, it will be entered into MATLAB and executed. To select more than one line, hold down the **Ctrl** key and click each line. Then you can right-click the mouse button, select copy, click in the command window, again right-click and select paste, to execute the selected commands.

The history file is separated into sections for each different MATLAB session, and each of these will have a time stamp. An entire session's history can be "collapsed" by clicking on the  symbol on the left of this time stamp.

There is an option on the Edit menu allowing you to clear your command history if you want to.

2.3 Built-in Functions

Although we will not discuss the creation of new functions until section 2.6, we will be *using* functions in the next few sections, and so we will need some functions which have already been defined. MATLAB has an enormous number of 'initially-known' mathematical functions (i.e. ones which are already there when you start MATLAB). These include the trigonometric functions

`sin`, `cos`, `tan`, `csc` (i.e. cosec), `sec`, `cot`

and their inverse functions

`asin`, `acos`, `atan`, `acsc`, `asec`, `acot`

and the hyperbolic functions

`sinh`, `cosh`, `tanh`, `csch` (i.e. cosech), `sech`, `coth`

and their inverse functions

`asinh`, `acosh`, `atanh`, `acsch`, `asech`, `acoth`

as well as, for example:

Function	Description	Example
<code>abs</code>	absolute value	<code>abs(-2)</code>
<code>sqrt</code>	square root	<code>sqrt(4)</code>
<code>max</code>	largest element in an array	<code>max([132,129,66,120])</code>
<code>min</code>	smallest element in an array	<code>min([132,129,66,120])</code>
<code>factorial</code>	factorial function	<code>factorial(12)</code>
<code>round</code>	round (up/down) to an integer	<code>round(3.5)</code>
<code>floor</code>	round down to an integer	<code>floor(-3.1)</code>
<code>ceil</code>	round up to an integer	<code>ceil(-3.1)</code>
<code>exp</code>	exponential	<code>exp(1)</code>
<code>log</code>	natural logarithm	<code>log(exp(2))</code>
<code>log10</code>	logarithm to base 10	<code>log10(100)</code>

Note that most of these function will work on one number, or if applied to a vector or matrix (see sections 2.4 and 2.8) to each element of the vector or matrix.

For a complete list of the initially-known MATLAB functions, use the Help browser (see section 1.5.1).

2.4 Basic Vectors

From its beginning, MATLAB was designed to work with matrices and vectors, as its name suggests. Everything in MATLAB is, potentially, a matrix: a number on its own is really a 1×1 matrix to MATLAB. Matrices and vectors are collectively called **arrays** in MATLAB.

We begin by looking at vectors.

14 CHAPTER 2. MATLAB COMMANDS

2.4.1 Row and Column vectors

There are two types of vectors in MATLAB: **row vectors** and **column vectors**. Both types of vector have square brackets enclosing the elements (also called components), and for both the command **size** will give the dimensions of the array, while **numel** gives the total number of elements in an array.

A row vector is printed as a row, and when you define one you separate its elements by either *commas* or *spaces*. A column vector is printed as a column, and you use *semi-colons* or new lines to separate the elements. For example

```
>> v=[ 1 3 , sqrt(21) ]
v =
    1.0000    3.0000    4.5826
>> w=[1 ; 3 ; sqrt(21) ]
w =
    1.0000
    3.0000
    4.5826
>> size(v)
ans =
     1     3
```

You can convert a row vector to a column vector and *vice versa* using the apostrophe or **back quote** ' — we call this **transposing**.

```
>> v=[ 1 3 sqrt(21) ] , v'
v =
    1.0000    3.0000    4.5826
ans =
    1.0000
    3.0000
    4.5826
```

To refer to an element of a vector, for example the third element of vector **v**, use an expression like **v(3)**. This can be extended to extract sequences of elements using the colon notation, see section 2.4.3. You can change the value of an entry with something like **w(2)=-3** as well. Note that in MATLAB all vectors (and matrices) are indexed from 1 (that is **v(1)** is the first element). You can also use **end** to refer to the last entry in a vector.

2.4.2 Vector arithmetic

Two vectors of the same size can be added and subtracted. In fact, you can make any linear combination of the vectors you want:

```
>> a=[1 -4 9 ]; b=[-2 2 3 ];
>> 2*a - 3*b
ans =
     8    -14     9
```

If the vectors are not compatible then you will get an error message.

You can apply functions to each element of a vector very simply:

```
>> v=[pi/4,pi/3,pi/2]; sin(v)
ans =
    0.7071    0.8660    1.0000
```

2.4.3 Colon and linspace

Entering a small vector by hand is not a problem, but MATLAB was designed for *big* problems, and often these involve vectors whose entries have some regularity, such as consecutive integers, or consecutive odd integers going downwards. If the entries of a vector are an *arithmetic* sequence, then you can use the **colon operator** or the **linspace** command to build the vector. Both of these produce row vectors, which can be transposed to column vectors with the apostrophe. For example

```
>> a=[1:4]
a =
    1     2     3     4
>> b = linspace(1,4,4)
b =
    1     2     3     4
>>c = [7:-2:1]
c =
    7     5     3     1
```

In general using $[a:b:c]$ where a , b and c are numbers will create a row vector whose first element is a , second element $a + b$ etc and whose last element is no greater than c (if $b > 0$, no less than c if $b < 0$). If there are only two numbers then MATLAB assumes the **increment** (b above) is 1, as in the first example.

On the other hand, **linspace**(a, b, c) creates a row vector with exactly c entries (100 if c is omitted) with entries equally spaced between a and b .

The colon operator can be used to extract more than one element at a time. Suppose vector w had 12 elements. Then the command

```
>> w( [ 1:2:5, 10:end ] )
```

will create a vector consisting of elements $w(1), w(3), w(5), w(10), w(11), w(12)$ only.

2.5 Plotting

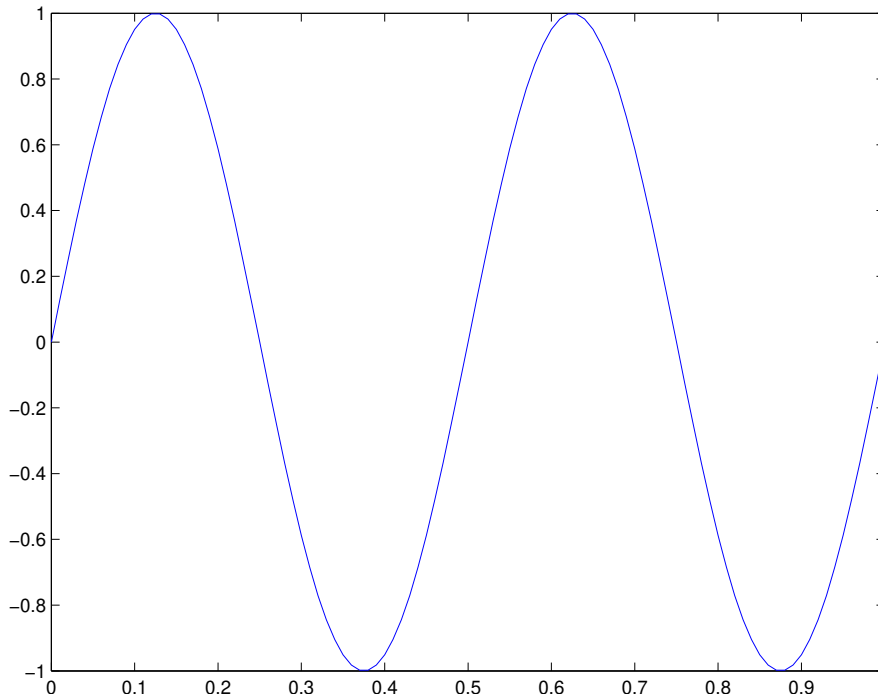
MATLAB has a large number of plotting commands, used for various special plots. We will only look at a few of the simplest and easiest.

2.5.1 plot command

The basic plotting command is **plot**.

The file containing figure 2.1 was produced with the following commands

```
>> x = linspace(0,1,101);
>> y = sin(4*pi*x);
>> plot(x,y);
>> print -dps 'sinplot.ps'
```

Figure 2.1: Plot of $\sin(4\pi x)$ over $[0, 1]$

The first command sets up a vector of 101 points along the x -axis, equally spaced between 0 and 1 (so 0.01 apart) and including both 0 and 1. Then we define $\sin(4\pi x)$ for each of these points. The `plot` command then plots the points (x_i, y_i) for each x_i in the vector `x` and corresponding y_i in vector `y`, then joins them up with straight lines: since the points are so close together the graph looks like a curve, but if you did this with points spaced 0.1 apart you would see the lines. The final command saves the plot into a PostScript file called `sinplot.ps`, which can be viewed using `ghostview` and/or printed out.

See section 2.7.3 for plotting parametric curves and more complicated functions.

2.5.2 ezplot

The `plot` command is very powerful, but often you just want to plot a function directly. The `ezplot` command can do this. A graph similar to figure 2.1 could have been produced with one command using

```
>> ezplot('sin(4*pi*x)', 0 , 1)
```

Note the use of the apostrophes here: they cannot be left out.

2.5.3 Style options

There are a large number of options you can use with `plot` to change how the graph is plotted or its colour. If you wanted to plot the graph of $\sin(4\pi x)$ with a red dashed line instead of the default blue solid line, for example, you would use the command

```
>> plot(x,y,'r--')
```

where the quotes make the third argument a **string**. The `r` is the colour and the `--` is the code for dashed. Some other possibilities are as below.

code	r	y	g	b	c	m	w	k
colour	red	yellow	green	blue	cyan	magenta	white	black
code	.	o	-	:	-.	--	x	*
style	points	circles	solid	dotted	dash-dot	dashed	x-marks	stars

The different styles and colours allow you to plot several graphs at once in a way you can tell them apart. To plot both $\sin(4\pi x)$ and $\cos(4\pi x)$ you could use (with x and y as above)

```
>> z = cos(4*pi*x);
>> plot(x, y, 'r-' , x , z, 'b--')
```

Here the sin plot is red and solid, the cos plot blue and dashed.

2.5.4 Titles, axes and grids

The `ezplot` command will automatically put a title on a graph — it uses the function as the title, not surprisingly. You can put a title on any plot using the `title` command, for example

```
title('My first plot');
```

adds the title “My first plot” to the current plot. Here the quotes define the title as a string.

Also, `ezplot` will label the x -axis with whatever you have used as the variable (x in the example above). To label axes for any other plot, use the commands `xlabel` and `ylabel` in the obvious manner. Finally, you can put a grid over a plot with `grid on`. Figure 2.2 shows what the earlier plot of $\sin(4\pi x)$ looks like after the additional commands

```
>> title('My plot of sin(4 \pi x)');
>> xlabel('x axis'), ylabel('y axis'), grid on
```

Note: The use of `\pi` to define the symbol π . This tells MATLAB that you want the correct symbol and not just the letters pi.

2.5.5 Specialised plot procedures

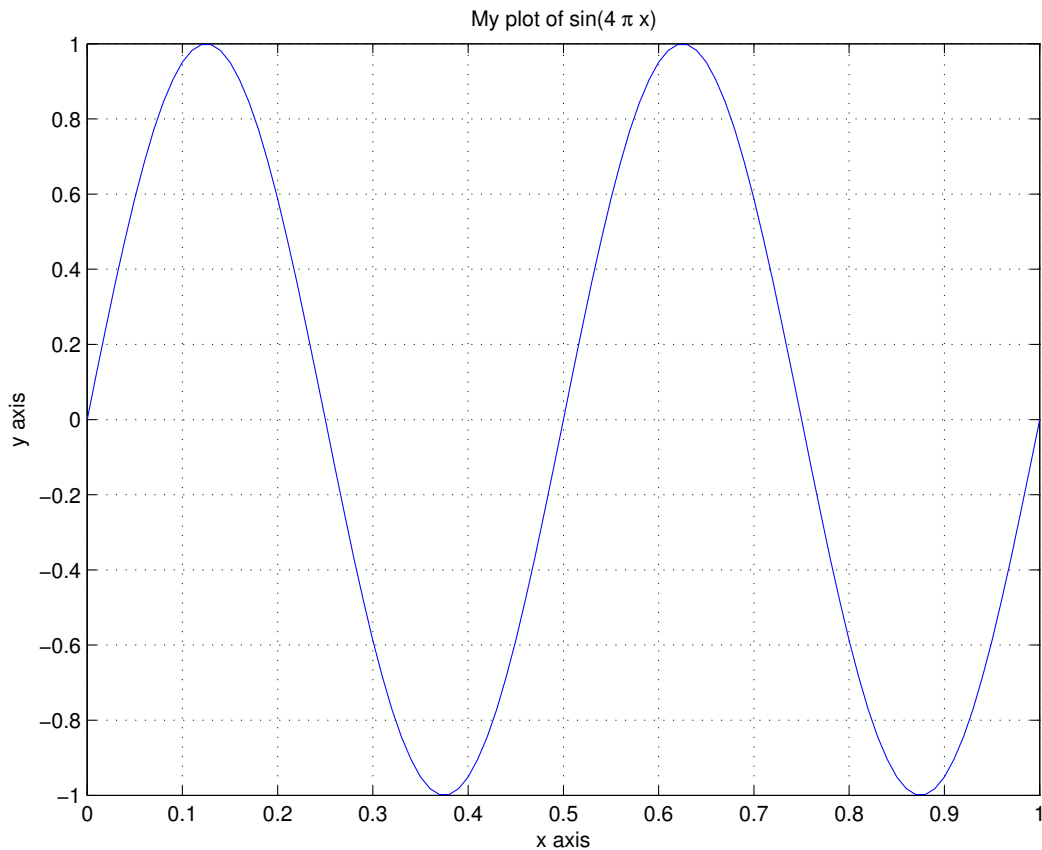
We mention one other useful specialised plotting command: `polar`, used to draw graphs in polar coordinates. For example, figure 2.3 is the result of the following commands

```
>> t = linspace(0, 2*pi, 200);
>> r = 1 + cos(t);
>> polar(t,r);
>> title('Cardioid')
```

2.6 M-files and New Functions

In section 1.3 we looked at an example of a **script file**, also called an **M-file**. This was an ordinary text (ASCII) file containing MATLAB commands; typing the name of the file (without the `.m` extension) causes MATLAB to run those commands as if you had typed them in.

Note that when you run a script file, MATLAB only prints the results of the commands, not the commands themselves. Use `echo on` to echo the commands; `echo off` turns

Figure 2.2: Second plot of $\sin(4\pi x)$ over $[0, 1]$

this echoing off. You can also use `what` to get a list of the M-files in your current directory (as well as finding out what MATLAB thinks is your current directory).

2.6.1 Function Files

A **function file** is another type of M-file, and is one way to define new MATLAB functions. To illustrate how these work, we consider an example:

Suppose you had r identical objects (coins perhaps) to be distributed to n people where each person can get more than one object: this is known as a **selection**. The number of ways you can do this can be shown to be $\frac{(n+r-1)!}{(n-1)!r!}$. The following commands creates a MATLAB function `selection` that calculates this number.

```
function [N] =selection(n,r)
%
% N=selection(n,r)
% number of ways N of distributing r objects among n
%
N = factorial(n+r-1)/(factorial(n-1)*factorial(r));
%%% end of file %%
```

To make use of this you have to save this sequence of commands into a file called

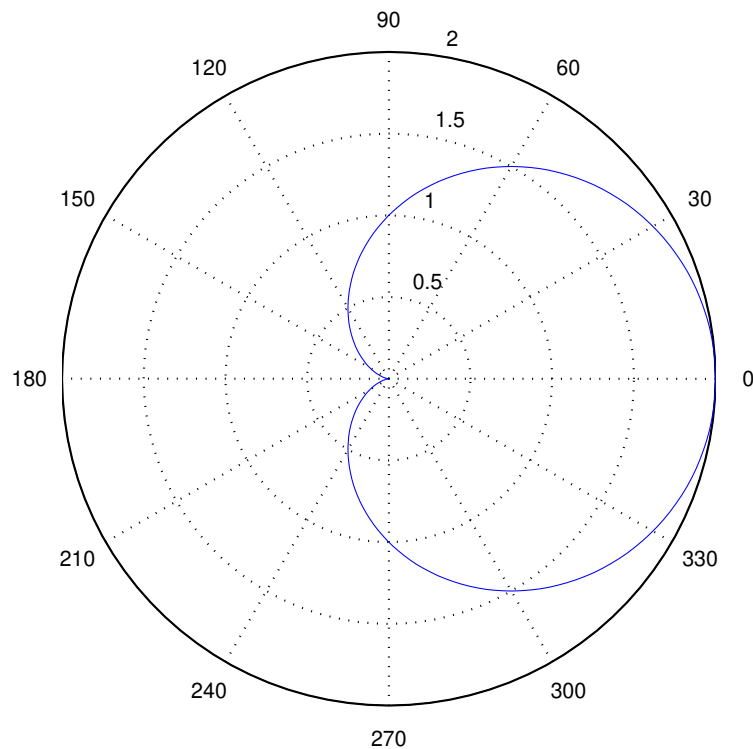


Figure 2.3: Plot of the cardioid $r = 1 + \cos(\theta)$ using polar

`selection.m` — the name of the file and the name of the function must be the same. To use the function, all you need to do is use it like any standard MATLAB command

```
>> selection(11,4)
ans =
    1001
```

There are several important points to be made

1. As already mentioned, the name of the file and the name of the function must be the same.
2. The first (non-comment) line must be of the form
`function [list of outputs] = name(list of inputs)`
3. Do not forget to document your function. The comment lines immediately after the opening line are printed out when you ask MATLAB for help on the function, so make them useful. This is why we have included the **calling sequence** in the comments.
4. It is possible to have more than one output variable (see the help pages on functions).

2.6.2 Anonymous Functions

An alternative way to define a function is to create an **anonymous function**. This is useful if you have a function (say a polynomial) that you wish to evaluate at several points

in your session but do not want to save as an M-file. These anonymous functions are also used in numerical integration (see section 2.9) and other places. A simple example will illustrate the idea:

```
>> polynom=@(t) t.^2-2.*t-3
polynom =
    @(t) t.^2-2.*t-3
>> polynom(-2)
ans =
    5
```

Note the use of the compulsory `@` symbol, which is used to create the **function handle**, in this case `polynom`. The parentheses immediately after the `@` contain the function parameters, which behave like the parameters of a function file. It is possible to have more than one parameter, or even no parameters. However, even if there are no parameters to pass to the function, you must include the parentheses to call the function (see the MATLAB help page on anonymous functions for an example).

2.7 Further Vectors

2.7.1 Ordinary Product

Given a row vector \mathbf{v} and a column vector \mathbf{w} both with the same number of elements, you can get MATLAB to calculate the usual matrix (or dot) product of \mathbf{v} and \mathbf{w} using a star for what is really matrix multiplication. So for example

```
>> v=[1 3 5 7]; w = [-2 ; 3 ; 4 ; -5];
>> v*w
ans =
    -8
```

An alternative is to use the MATLAB command

```
>> dotprod(v, w)
```

2.7.2 Array Arithmetic

One of MATLAB more useful but unusual features is a heavy reliance on **array operators**. These are operations that are applied *element-by-element* to an array (a vector or matrix). We have already noticed that we can say, for example, `sin(v)` for a vector \mathbf{v} and get a vector whose entries are the sines of the entries of \mathbf{v} .

We can apply more basic functions to the elements of an array (or more than one array, as appropriate) by using **array operators**, sometimes called **dot operators**, as they use a dot. For example, we can create a vector whose elements are the cubes of the first 5 integers by the command

```
>> [1:5].^3
```

Note the dot: `.^3` means cube *each member of the array separately*. It's not the same as cubing an array in the usual mathematical sense you would use for, say, square matrices.

Other examples include `.*`, which can be applied to two arrays of exactly the same shape and will multiply corresponding entries together, and `./` which will similarly divide corresponding entries. For example

```
>> v = [1 2 3 4]; w = [2 3 5 7];
>> v.*w
```

```
ans =
     2     6    15    28
>> v./w
ans =
    0.5000    0.6667    0.6000    0.5714
```

2.7.3 More on plotting

We can use the array arithmetic mentioned above to plot more complicated functions, for example polynomials, or something like e^{-x^2} .

So we could plot $x^3 - 2x^2 + 3$ over $[-2, 2]$ with

```
>> x = linspace(-2,2,200); y = x.^3-2*x.^2 + 3; plot(x,y)
```

And plot e^{-x^2} over $[-2, 2]$ with

```
>> x = linspace(-2,2,200); y = exp(-x.^2); plot(x,y)
```

But we can also plot *parametric* functions this way. As a simple example, suppose we want to plot the curve given by $x = t^2$, $y = t^3$ for $-1 \leq t \leq 1$. Then we could use the commands

```
>> t=-1:0.01:1;
>> plot(t.^2, t.^3)
```

2.8 Matrices and Linear Equations

We next turn to the mathematical objects that give MATLAB its name: **matrices**. A $p \times q$ matrix is a rectangular array of numbers, with p rows and q columns, for example

$$A = \begin{pmatrix} 1 & 2 & 3 \\ 6 & 7 & -2 \end{pmatrix}$$

is a 2×3 matrix.

2.8.1 Definitions

To enter the matrix A above we follow the same syntax as for vectors. We enter each row with spaces (or commas) separating the entries and with semi-colons separating the rows (that is, defining the columns). So we can enter the matrix A above with

```
>> A = [ 1  2  3 ; 6  7  -2 ]
```

Alternatively, you can take a new line for each new row:

```
>> A = [ 1  2  3
        6  7  -2 ]
```

You can use the colon to create rows of a matrix as well, so the first row of A could have been defined using `1:3`.

The apostrophe can be applied to a matrix to get the **transpose matrix**: all the rows are swapped to columns and *vice versa*. There are other commands in MATLAB to rearrange matrices, such as `flipud` and `flipr1` will flip a matrix up-down (around a horizontal axis) and right-left (around a vertical axis) respectively — compare these to the transpose, which is a flip around a diagonal.

22 CHAPTER 2. MATLAB COMMANDS

You can get the size of a matrix using the command `size`, for example

```
>> size(A)
ans =
     2     3
```

`size` is an example of a function that returns a matrix: a 1×2 matrix in fact.

Entries of a matrix can be extracted or changed just as for a vector, although you need to give two indices of course. For example `A(2,1)` extracts the entry in the second row, first column of A (if A has a second row). Similarly to vectors you can extract more than one element using the colon, and in this way create submatrices. Once again, the indexing begins from 1 and the keyword `end` can be used for the last entry, see section 2.4.1.

For example

```
>> B = [1 3 5 ; 2 4 6 ; 4 9 16 ];
>> C = B( 2:3 , : )
C =
     2     4     6
     4     9    16
```

Note that the colon on its own is equivalent to `1:end` and means all the rows (or columns) of the matrix.

In many applications matrices have some sort of structure and are most easily made by being built up from smaller matrices and/or vectors. One obvious example is creating the augmented matrix for a system of linear equations (see section 2.8.5 for solving linear equations). However, in MATLAB you can not only **augment** matrices/vectors (put them side by side) but also **stack** them (put one on top of the other). For example:

```
>> A=[1 2; 3 4]; v=[-1; -1]; B= [-3 -2 ; 0 -1 ];
>> [A v] % augmenting
ans =
     1     2    -1
     3     4    -1
>> [A ; B] % stacking
ans =
     1     2
     3     4
    -3    -2
     0    -1
```

2.8.2 Special matrices

MATLAB includes several useful commands for creating special types of matrices:

1. For a 3×3 (say) identity matrix, use `eye(3)`
2. For a 3×4 (say) matrix of zeros use `zeros(3,4)`
3. For a 3×2 (say) matrix of ones use `ones(3,2)`

4. To create a diagonal matrix whose entries are the elements of the vector \mathbf{v} use `diag(v)`

These matrices can be particularly useful in stacking and augmenting matrices.

2.8.3 Standard Matrix Arithmetic

For the usual mathematical product of two matrices, or a matrix and a vector, use the `*` symbol on its own. The two arrays you multiply must have compatible dimensions. Also, do not forget that $\mathbf{A*B}$ and $\mathbf{B*A}$ will in general give different results

```
>> A = [1 2 3; 4 5 6];
>> B = [0 1 ; 1 0 ; 0 0];
>> A*B
ans =
     2     1
     5     4
>> B*A
ans =
     4     5     6
     1     2     3
     0     0     0
```

Later on in your courses you will need to use the various MATLAB commands for calculating with matrices. For example,

```
inv(A)      for the matrix inverse;
det(A)      for the determinant;
eig(A)      for calculating eigenvalues and eigenvectors;
rank(A)     for the rank.
```

2.8.4 Matrix array arithmetic

Just as in the case of vectors, MATLAB allows you to operate on each element of a matrix individually, so for example `exp(A)` will give a matrix whose (i, j) th entry is $e^{a_{ij}}$. In later year courses you may come across the matrix exponential, (`expm` in MATLAB) which is a completely different thing, used for solving systems of differential equations.

Also, the “dot” operators work on matrices. So `A.^2` will square every entry of matrix A . This is *very different* to `A^2`, which is shorthand for $\mathbf{A*A}$ of course.

2.8.5 Systems of Linear Equations

There are special built in procedures `\` and `rref` for solving systems of linear equations.

The backslash or **left division operator** is used for solving a system of equations of the form $\mathbf{Ax} = \mathbf{b}$. For example

```
>> A = [ 3  7 ; 2  5]; b = [1 ; 2];
>> A\b
ans =
```

24 CHAPTER 2. MATLAB COMMANDS

```
-9.0000  
4.0000
```

This is mathematically the same as calculating $A^{-1}\mathbf{b}$ (you could solve the problem with `inv(A)*b` in MATLAB) but left division is generally faster and uses some sophisticated techniques appropriate for solving systems with floating point numbers, so is a better way of finding the solution, as well as being easier to type. However, be aware that left division will return a result *even if the system is actually inconsistent* (has no solutions). In this case the answer you get is the **least squares best fit** to a solution, since this is what is usually wanted in such situations, as you may see in future courses. You need to use `rank(A)` or something similar to check you have a unique solution if you are uncertain.

If you actually want to do a row reduction (Gaussian elimination), the command `rref(A)` will reduce A to reduced row echelon form. If A were the augmented matrix of a system of linear equations (see page 22), then the last column of the reduced row echelon form is a solution to the system.

2.9 Calculus

MATLAB is not capable of doing true calculus on its own — for that you would need to use a Computer Algebra System such as MAPLE. But MATLAB can do some calculus calculations, for example **numerical integration** also called **quadrature**: finding the approximate value of a definite integral.

The simplest commands to use are `trapz` and `quad`. The former uses the trapezoidal rule and the latter Simpson's Rule to calculate an integral. Note that `quad` uses an adaptation of Simpson's Rule to make it faster and more accurate. For example, suppose you wished to approximate the value of $\int_0^\pi \sin(x^2) dx$ by Simpson's rule using an absolute error tolerance of 10^{-15} . Then we begin by defining an anonymous function (section 2.6.2)

```
>> format long  
>> fcn=@(x) sin(x.^2);  
>> quad(fcn,0,pi,10^(-15))  
ans =  
0.77265171269007
```

We see here the use of the function handle `fcn`: it literally gives us a “handle” on the anonymous function so we can use it in `quad`.

2.10 Programming Considerations

So far, the examples we have discussed have been essentially using MATLAB as a (sophisticated) interactive calculator. However, MATLAB is *programmable*, in the sense that you can get it to do repeated calculations and make choices. You may be expected to be able to do some simple programming in this sense in your course, and if you are to make proper use of MATLAB's power you need to be able to use the two constructs we now turn to: **conditionals** and **loops**.

2.10.1 Logicals

Before we look at `if` statements and loops, we need to consider how MATLAB will be handle true/false, in other words how MATLAB does **boolean algebra**. A variable or command that results in true/false is known as a **boolean**. Quite simply, in MATLAB

the integer 0 represents false and 1 represents true. Suppose you had a variable x and you wanted to test to see if it is greater than ten (without actually looking at it). In MATLAB this would look like

```
>> x>10
ans =
     1
```

and the value of **ans** tells you that x is greater than 10.

There are 5 other **relational operators** apart from $>$, illustrated below. Note that they can all be used on arrays and then are applied elementwise, as is typical. Suppose we have a vector defined by

```
>> x = [0 -1 2 4]
ans =
     0     -1     2     4
```

then we have the following possibilities

command	result	description
$x==2$	[0 0 1 0]	entries equal to 2
$x>2$	[0 0 0 1]	strictly greater than 2
$x>=2$	[0 0 1 1]	greater than or equal to 2
$x<2$	[1 1 0 0]	strictly less than 2
$x<=2$	[1 1 1 0]	less than or equal to 2
$x\sim=2$	[1 1 0 1]	not equal to 2

Note that the 2 on the right hand side is assumed to be an array of the right size all of whose entries are 2.

For more advanced uses of logicals we need the logical operators $\&$ (and), $|$ (or) and \sim (not). So with the vector x above we get

```
>> x>=0 & x <=2
ans =
     1     0     1     0
>> x<0 | x>1
ans =
     0     1     1     1
>> ~(x>2)
ans =
     1     1     1     0
```

2.10.2 If Statements

An `if...elseif...end` statement is known as a **conditional**, a **branch** or a **fork** — control is sent down one of two possible paths depending on the truth value of a boolean statement. For example

```
if (x>3) | (y<=2) ... end
```

26 CHAPTER 2. MATLAB COMMANDS

```
if (a>b) & (c>d) ... end
```

If the boolean is true then MATLAB runs the commands after the boolean. If you want to, you can make MATLAB do something else if the boolean is false, or do nothing; you do the former with an **else** clause. For example, the following commands find the absolute value of a real number:

```
if x>=0
    x
else
    -x
end
```

You can **nest** if statements as well; the general form of the **if** command is something like

```
if condition1
    commseq1
elseif condition2
    commseq2
elseif condition3
    commseq3
else
    commseq4
end
```

2.10.3 Loops

Suppose that you want to execute a set of MATLAB commands several times, changing the value of one variable n at each repetition. This is called creating a **loop**, and is very common in scientific and financial programming.

The way you create the loop depends on whether you know in advance exactly how many times you want to repeat the commands or not. If you know that you want to repeat the commands 100 times then you can use a construction of the type

```
for n = 1:100
    commands
end
```

The `1:100` is the colon operator we met before, and can be generalised here too, so `100:-2:0` would have **n** run through even numbers backwards. Also note that unlike many other languages, MATLAB allows non-integer increments in loops, so `h=0:0.1:1` is legal. The **end** is essential to tell MATLAB where the commands to be repeated end.

If you do not know how many repetitions you want to make then you will have to tell MATLAB to keep repeating until some condition is no longer satisfied, using a construction of the type

```
while a<= b
    commands
end
```

To illustrate, we give two examples. Firstly, consider the following commands

```
>> t=linspace(0,2*pi,200);
>> for n = 0.5:0.5:4
    polar(t,2+n*sin(t))
    pause
end
```

This block will plot various polar curves known as **limaçons**, with the **pause** statement making it stop after each plot until you press any key (a message at the bottom of the main MATLAB window tells you this). Note also that there is a message at the bottom of the MATLAB window as you enter the commands in the loop, telling you to “continue entering statement”.

Secondly, suppose you wish to find all the Fibonacci numbers up to and including the first one that is larger than 1000. The natural way to do this is to calculate each number, check to see that it is smaller than 1000, if not, then calculate the next one and repeat. But we cannot check the size of the number at the end of a loop in MATLAB, only at the start. To get around this, we do the following:

```
>> F(1)=0 ; F(2)=1 ; n=2;
>> while F(n)<=1000
    F(n+1) = F(n)+F(n-1);
    n=n+1;
end
```

At the end of this loop **F(n)** will contain the first Fibonacci number greater than 1000, which is 1597, and the vector **F** will have all the calculated Fibonacci numbers in it. Note that the semi-colon after the each statement in the block suppresses the printing of the intermediate values.

2.10.4 Other Control Structures

MATLAB has other commands used in programming, which we will leave you to explore yourself if you need to use them.

For more general branching than is provided with **if** statements, MATLAB provides the **switch** construction, where control can be sent down any number of different forks depending on the value of a variable.

The command **break** in a **for** or **while** loop stops the loop and either returns to the input prompt or execution continues with the command after the **end**.

An **error** command can be used to abort a function or script file, sending a message as it does so. Similarly, a **return** in a function stops the execution, returning to the input prompt (or invoking function, if the return is in a function called by another function).

There are also the commands **input**, **keyboard** and **menu** (as well as **pause**, which we saw earlier) which can be used to make functions interactive. Again, for details and examples, see the Help pages.

Note that it is always much easier to understand code containing control statements like **for** if they are **indented**, as we have shown here. This can easily be done using the MATLAB editor: use the mouse to highlight the code with the control statements and then select the option Smart Indent from the Text menu of the MATLAB editor.

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