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3 Observations of submesoscale variability and frontal subduction  
4 within the mesoscale eddy field of the Tasman Sea  
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**Abstract**

Submesoscale lenses of water with anomalous hydrographic properties have previously been observed in the East Australian Current (EAC) system, embedded within the thermocline of mesoscale anticyclonic eddies. The waters within these lenses have high oxygen content and temperature-salinity properties that signify a surface origin. However, it is not known how these lenses form. This study presents field observations that provide insight into a possible generation mechanism via subduction at upper ocean fronts. High-resolution hydrographic and velocity measurements of submesoscale activity were taken across a front between a mesoscale eddy dipole downstream of the EAC separation point. The front had  $O(1)$  Rossby number, strong vertical shear, and flow conducive to symmetric instability. Frontogenesis was measured in conjunction with subduction of an anticyclonic water parcel, indicative of intrathermocline eddy formation. Twenty-five years of satellite imagery reveals the existence of strong mesoscale strain coupled with strong temperature fronts in this region, and indicates the conditions that led to frontal subduction observed here are a persistent feature. These processes impact the vertical export of tracers from the surface and dissipation of mesoscale kinetic energy, implicating their importance for understanding regional ocean circulation and biological productivity.

54        **1. Introduction**

55        Over the past decade, a succession of numerical and observational studies have revealed the rich  
56        tapestry of submesoscale ocean currents that have horizontal scales of  $O(0.1-10)$  km and evolve  
57        and decay much faster than their mesoscale counterparts (e.g. Capet et al., 2008; Thompson et  
58        al., 2016; see McWilliams (2016) for a review). While submesoscale ocean features were  
59        observed several decades earlier (e.g. Flament et al., 1985; Munk et al., 2000), it was not until  
60        recently that the global extent, complexity and importance of this scale class has been realized  
61        (Mahadevan, 2016; Su et al., 2018; Torres et al., 2018). Submesoscales provide a pathway for  
62        the cascade of energy from the large scale, where it is input by atmospheric forcing, to the  
63        microscale, where it is dissipated, and in modulating the mesoscale field (Molemaker et al.,  
64        2010). They are also associated with enhanced turbulence, lateral/vertical mixing and strong  
65        vertical velocities (Klymak et al., 2016; D'Asaro et al., 2011; Shcherbina et al., 2015) and  
66        therefore influence primary productivity and atmospheric exchange (Mahadevan, 2016; Omand  
67        et al., 2015).

68               Submesoscale currents form through a variety of mechanisms, including mixed layer  
69        instabilities (Boccaletti et al., 2007), mesoscale frontogenesis (Spall, 1997) and topographic  
70        wakes (Molemaker et al., 2015). As such, they exhibit strong spatial and temporal  
71        inhomogeneity with considerable variation both geographically and seasonally (Sasaki et al.,  
72        2014; Callies et al., 2015; Rocha et al., 2016). Difficulties in measuring these intermittent small-  
73        scale features have restricted observational studies to a limited number of localized regions, via  
74        ship-based field campaigns (e.g. CARTHE – Poje et al., 2014; OSMOSIS – Thompson et al.,  
75        2016; SMILES – Adams et al., 2017, LatMix – Shcherbina et al., 2015), repeat ship-of-  
76        opportunity sampling (Wang et al., 2010; Qiu et al., 2017; Chereskin et al., 2019), or coast-based

77 high frequency (HF) radar (Kim et al., 2011; Archer et al., 2015; Schaeffer et al., 2017; Yoo et  
78 al., 2018). Therefore, many regions of the world remain unsampled with respect to submesoscale  
79 ocean variability.

80 Many of these studies have highlighted the critical role of frontal zones in transferring  
81 kinetic and potential energy from the mesoscale current field to submesoscales. Fronts can form  
82 by the mesoscale stirring of lateral density gradients; frontogenesis occurs when the density  
83 gradients are sharpened through lateral strain. As the front sharpens, an ageostrophic secondary  
84 circulation can develop to drive the along-front flow back to thermal wind balance through re-  
85 stratification (Hoskins, 1982). This takes the form of a single overturning cell that can drive  
86 vertical exchange between the mixed layer and interior. Submesoscale instabilities can feed off  
87 the local potential and kinetic energy of the intensifying front. These instabilities are strongly  
88 influenced by the atmosphere – air-sea heat fluxes and frictional wind forcing can both act to  
89 further de-stabilize the water column. The particular flavor of submesoscale instability that  
90 dominates is dependent on the distributions of vorticity and density gradients, which can incite  
91 gravitational instability (Haine and Marshall, 1998), centrifugal/inertial instability (Molemaker et  
92 al., 2015), symmetric instability (Thomas et al., 2013), and mixed layer baroclinic instability  
93 (Stone, 1970; Boccaletti et al., 2007; Fox-Kemper et al., 2008).

94 During frontal instability, surface water can be subducted along isopycnals, develop  
95 anticyclonic vertical vorticity, and separate from the mixed layer to form an intrathermocline  
96 eddy (hereafter ITE; Spall, 1995; Thomas, 2008; also termed a submesoscale coherent vortex –  
97 McWilliams, 1985). ITEs are submesoscale anticyclonic eddies observed throughout the  
98 stratified interior of the ocean (Dugan et al., 1982; Kostianoy and Belkin, 1989). They are  
99 characterized by their small length scales, well-mixed and anomalous water properties, long

100 lifetimes, and large propagation distances. For these reasons, the cumulative effect of ITEs in the  
101 world's oceans has a potentially significant impact on the transport and distribution of heat, salt,  
102 and other tracers. In addition to frontal instability, other mechanisms for ITE generation include:  
103 bottom drag on boundary currents at topographic features (e.g. D'Asaro, 1988; Gula et al., 2019),  
104 diapycnal mixing and geostrophic adjustment (e.g. McWilliams, 1985), and baroclinic instability  
105 of an undercurrent (e.g. Jungclauss, 1999). Despite modeling studies that can explain the ITE  
106 generation mechanism via frontal instability and subduction (Spall, 1995; Thomas, 2008), there  
107 are few direct observations of this process (Lee et al., 2006). However, such a mechanism may  
108 play an important role in ocean-atmosphere exchange, by exporting near-surface water masses  
109 influenced by atmospheric forcing down into the ocean interior (Klein and Lapeyre, 2009).

110         In the Tasman Sea east of Australia, Baird and Ridgway (2012; hereafter BR12)  
111 identified submesoscale lenses of anomalous water at depth, embedded within mesoscale  
112 anticyclonic eddies. The water mass characteristics of these lenses revealed their origin as Bass  
113 Strait water, but BR12 did not observe how they form. Brannigan et al. (2017), based on results  
114 of high-resolution idealized simulations, conjectured that the Bass Strait lenses observed by  
115 BR12 may have formed due to submesoscale instabilities in the mixed layer of mesoscale eddies,  
116 but no observations of this process have been made.

117         Here we present high-resolution in-situ observations of submesoscale processes in the  
118 Tasman Sea (Fig. 1) taken during a research cruise in austral late winter/early spring 2017. The  
119 measurements were made across a frontal zone separating an anticyclonic warm core eddy and  
120 cyclonic cold core eddy, immediately south of the East Australian Current (EAC) separation  
121 zone (Fig. 1). Our analysis indicates the presence of frontogenesis-induced submesoscale  
122 subduction, symmetric instability, and the formation of an intrathermocline eddy. These

123 observations lend support to the theory that such submesoscale lenses may form regularly  
124 between mesoscale eddies in the Tasman Sea due to submesoscale instabilities in the mixed  
125 layer.

## 126 **2. Study region**

127 Ocean circulation in the Tasman Sea is dominated by the presence of the EAC, the western  
128 boundary current (WBC) of the South Pacific subtropical gyre (Oke et al., 2019). The EAC is  
129 known for being the most variable of WBCs globally, with a large eddy kinetic energy (EKE) to  
130 kinetic energy (KE) ratio (Godfrey, 1980; Archer et al., 2017). The EAC flows along the  
131 continental slope of east Australia until it separates from the coast typically between 30-32° S  
132 (Cetina-Heredia et al., 2014), flowing eastward as the Tasman Front. At the separation point,  
133 mesoscale anticyclonic eddies intermittently shed from the EAC retroflection and interact with  
134 cyclonic eddies from offshore (Fig. 1). Local wind forcing has been shown to influence the  
135 timing of EAC eddy shedding events, whereas remote wind forcing appears to have limited  
136 impact on this intrinsically variable WBC system (Bull et al., 2017). The area immediately south  
137 of where the EAC separates has been termed ‘eddy avenue’ for its abundance of energetic  
138 mesoscale eddies with exceptionally large anomalies in sea surface temperature (SST) and  
139 chlorophyll-a (Everett et al., 2012). For this reason, the focus of earlier studies in the region was  
140 to characterize the variability and dynamics of mesoscale eddies, from a statistical perspective as  
141 well as individual case studies (Macdonald et al., 2013; Everett et al., 2015; Roughan et al.,  
142 2017; Oke et al., 2019).

143 Several recent studies have investigated submesoscale variability of the EAC as it flows  
144 along the continental shelf upstream of its separation (Roughan et al., 2017; Schaeffer et al.  
145 2017; Mantovanelli et al., 2017; Archer et al., 2018). Submesoscale flow in this regime is

146 characterized by instability of the meandering EAC and generation of frontal eddies (Schaeffer et  
147 al., 2017). These eddies have  $O(1)$  Rossby number, and asymmetric distributions of vorticity and  
148 divergence. They occur intermittently all year round, and are associated with upwelling and  
149 elevated chlorophyll-a concentrations (Roughan et al., 2017; Schaeffer et al., 2017). Archer et al.  
150 (2018) used over 4 years of high-resolution (1.5 km) HF radar observations in this upstream  
151 region to explore surface current variability; in EKE wavenumber spectra they identified a  $k^{-3}$   
152 power spectral slope, which indicates the dominance of mesoscale motions, and little-to-no  
153 seasonality in submesoscale variance. Poleward of where the EAC separates from the coast,  
154 satellite imagery reveals submesoscale features (Fig. 1), yet there have been no dedicated in situ  
155 observations to determine the subsurface hydrographic and velocity structure of these scales. The  
156 measurements analyzed here are the first to focus on these upper ocean submesoscales poleward  
157 of the EAC separation.

### 158 **3. Data and methods**

#### 159 **a. Shipboard observations**

160 The primary observations used in this study were collected during a research cruise in the  
161 Tasman Sea, austral late winter/early spring (31 August to 18 September 2017), aboard the R/V  
162 Investigator. Standard shipboard underway measurements used include: salinity and temperature  
163 from a thermosalinograph (Sea-Bird-SBE 21) with measurement depth of 2 m within the drop  
164 keel, and wind speed and direction from a wind vane (RM Young Wind Sensor Type 05108) on  
165 the starboard foremast. Vertical profiles of conductivity (SBE4C), temperature (SBE3T),  
166 pressure, and dissolved oxygen (DO; SBE43) were made by a Seabird SBE 911, down to a depth  
167 of 1000 m at 1 dbar intervals. The voyage data is quality controlled by the Australian Marine  
168 National Facility staff using their standard procedures

169 (<https://doi.org/10.4225/08/5a964b9041903>). Potential density, absolute salinity, conservative  
170 temperature, and the thermal expansion coefficient were calculated using the TEOS-10 toolbox  
171 (McDougall and Barker, 2011).

172 Vertical profiles of horizontal currents were collected down to a depth of ~800 m with 8  
173 m vertical bins and 1.2 km horizontal spacing, using a ship-mounted acoustic Doppler current  
174 meter (S-ADCP; RDI OS75 kHz narrowband operation). The University of Hawaii's Common  
175 Ocean Data Access System (CODAS) was used for post-processing, including corrections for  
176 ship speed and heading, with data output as 5 min averages from 1 Hz sampling frequency.  
177 Unless otherwise stated, all velocity is rotated to along the ship track (u-component) and across-  
178 track (v-component), which is approximately equivalent to being across-front (u) and along-front  
179 (v), since the ship passed the frontal zone almost perpendicular to its axis (within 4°). We tested  
180 the sensitivity of our results to this rotation angle, comparing velocity data rotated to the surface  
181 front velocity orientation as well as the 200-m depth-averaged front orientation; the results are  
182 not sensitive to these changes.

183 A Triaxus (a vertically profiling towed body) was deployed to map the hydrographic  
184 structure across the front at high resolution (on 12 September 14:46 to 22:27 Z). It was equipped  
185 with a dual-sensor Seabird SBE 911, collecting temperature, conductivity, pressure, and DO.  
186 Chlorophyll was measured by an Eco-Triplet payload. The Triaxus was towed at a speed of 8  
187 knots (~4 m s<sup>-1</sup>), approximately 1.5 km behind the vessel, in a sawtooth pattern with horizontal  
188 spacing of ~ 2 km between bottom turns, over vertical dives of ~200 m. This equates to a time  
189 lag between the S-ADCP and Triaxus measurements of approximately 6 minutes. The depth of  
190 the dives was progressively increased throughout the deployment to capture the base of the  
191 mixed layer, as the ship moved from the cold core eddy to the warm core eddy. All Triaxus-



192 measured variables are gridded horizontally ( $dx \sim 1$  km) and vertically ( $dz = 1$  m) by linearly  
193 interpolating between successive up- and down-casts.

#### 194 **b. Satellite imagery**

195 To characterize the mesoscale eddy field, we use satellite-measured absolute dynamic  
196 topography (ADT) and geostrophic currents obtained from the DUACS-DT2014 L4 gridded  
197 multi-mission altimeter daily product on a  $0.25^\circ \times 0.25^\circ$  resolution grid (Pujol et al., 2016).  
198 Backward-in-time Finite-Size Lyapunov Exponents (FSLE;  $\text{day}^{-1}$ ) are supplied by AVISO at a  
199 horizontal resolution of  $0.04^\circ$ , calculated from geostrophic velocities. FSLEs are a Lagrangian  
200 diagnostic measuring the exponential rate of separation ( $\lambda$ ) between two neighboring particles  
201 during a time of advection ( $t$ ), defined as  $\lambda = t^{-1} \log(\delta_0/\delta_f)$ , where  $\delta_0$  ( $\delta_f$ ) is the initial (final)  
202 separation distance (d'Ovidio et al., 2004). AVISO-defined parameters are:  $\delta_0 = 0.02^\circ$ ,  $\delta_f = 0.6^\circ$ ,  
203 with a maximum integration window of 200 days. FSLEs are used here to diagnose the strain  
204 field (Vaugh et al., 2008), and are positively correlated with gradients of buoyancy at the  
205 submesoscale, as shown in the Antarctic Circumpolar Current (ACC) (Siegelman et al. 2019).  
206 Since we use several satellite SST and chlorophyll-a datasets, we note the data source when used  
207 in the text.

#### 208 **c. Diagnostic calculations**

209 The satellite data is on a Cartesian longitude-latitude grid, so we calculate both horizontal  
210 gradient terms ( $\partial/\partial x$  and  $\partial/\partial y$ ). However, for in-situ measurements, horizontal gradients can  
211 only be calculated along the ship track. Therefore, we orientate the coordinate system along-  
212 track ( $x$ -direction) and across-track ( $y$ -direction), and assume that across-front gradients ( $\partial/\partial x$ )  
213 are significantly larger than along-front gradients ( $\partial/\partial y \rightarrow 0$ ), which is a reasonable  
214 approximation based on the high-resolution SST imagery depicting a nearly straight front during

215 the in situ sampling (see §5). The z-coordinate is positive upwards. We calculate all gradients  
216 using a centered second-order differencing scheme.

217 *i. In-situ velocity gradient tensor*

218 From the horizontal velocity gradient tensor, we calculate vertical relative vorticity

219 
$$\zeta = \frac{\partial v}{\partial x}, \quad [1]$$

220 horizontal divergence

221 
$$\delta = \frac{\partial u}{\partial x}, \quad [2]$$

222 and strain

223 
$$\sigma = \left[ \left( \frac{\partial u}{\partial x} \right)^2 + \left( \frac{\partial v}{\partial x} \right)^2 \right]^{1/2}. \quad [3]$$

224 *ii. In-situ potential vorticity calculation*

225 Ertel potential vorticity (hereafter PV, or denoted by the symbol  $q$ ) can be used as a diagnostic to  
226 indicate the susceptibility of the flow to instability (e.g., Hoskins, 1974; Thomas et al., 2008). In  
227 its full form it is:

228 
$$q = (f + \nabla \times \mathbf{u}) \cdot \nabla b \quad [4]$$

229 where  $\mathbf{u} = (u, v, w)$  is the velocity vector,  $f$  is the Coriolis parameter, and  $b = -g\rho'/\rho_0$  is the  
230 buoyancy ( $g$  is acceleration due to gravity,  $\rho'$  is a density perturbation, and  $\rho_0$  is a reference  
231 density, taken here as the full-depth mean). When PV has the opposite sign of  $f$  ( $f q < 0$ ), the  
232 flow is inherently unstable (Thomas et al., 2013). PV can be decomposed into two main terms:

233 
$$q = q_{vert} + q_{bc} \quad [5]$$

234 
$$q_{vert} = (f + \zeta)N^2 \quad [6]$$

235 
$$q_{bc} = \left( -\frac{\partial v}{\partial z} \right) \frac{\partial b}{\partial x} = -\frac{\partial v}{\partial z} M^2 \quad [7]$$

236 where  $N^2 = \partial b / \partial z$  is the vertical buoyancy gradient, and  $M^2 = \partial b / \partial x$  is the horizontal  
 237 buoyancy gradient.  $q_{vert}$  relates to the vertical component of absolute vorticity ( $f + \zeta$ ) and  $N^2$ ,  
 238 and  $q_{bc}$  relates to the horizontal relative vorticity (vertical shear) and  $M^2$ . Gravitational  
 239 instability can occur when  $N^2 < 0$ . If the water column is stably stratified ( $N^2 > 0$ ) then for  $f q_{vert} <$   
 240  $0$ , inertial or centrifugal instability may occur. However, if  $f q < 0$  is due to the baroclinic term,  $f$   
 241  $q_{bc} < 0$ , then symmetric instability can occur (Thomas et al., 2013). When the frontal flow is  
 242 approximately in thermal wind balance (i.e. the vertical shear is geostrophic  $\partial v_g / \partial z = 1 /$   
 243  $f \partial b / \partial x$ ),  $q_{bc}$  can be expressed as (Thomas et al., 2008):

$$244 \quad q_{bc}^g = -f \left( \frac{\partial v_g}{\partial z} \right)^2 = -\frac{1}{f} \left( \frac{\partial b}{\partial x} \right)^2 = -\frac{M^4}{f} \quad [8]$$

245 Thus  $f q_{bc}^g$  is a negative definite quantity so that the baroclinicity of the thermal wind shear  
 246 always acts toward  $f q < 0$  (i.e., the horizontal vorticity of the geostrophic shear is “anticyclonic”).  
 247 Therefore, symmetric instability can occur when the magnitude of  $q_{bc}^g$  exceeds  $q_{vert}$ . To  
 248 incorporate the effect of flow curvature, we calculate PV in cylindrical coordinates (Shakespeare,  
 249 2016):

$$250 \quad q_{cyl} = \left( f + \frac{\partial v_\theta}{\partial r} + \frac{v_\theta}{R} \right) \frac{\partial b}{\partial z} - \frac{1}{f} \left( \frac{\partial b}{\partial r} \right)^2 \quad [9]$$

251 where  $v_\theta$  is the radial velocity,  $r$  is the radial coordinate, and  $R$  is the radius of curvature.

### 252 *iii. Atmospheric forcing*

253 Frictional forces associated with wind forcing over an ocean front can modulate the PV (and so  
 254 potentially drive instability) as captured by the Ekman buoyancy flux:

$$255 \quad EBF = \frac{\tau_y}{\rho_0 f} \frac{\partial b}{\partial x} \Big|_{z=0}, \quad [10]$$

256 where  $\tau_y$  is the along-front component of the wind stress. Winds directed along the front in the  
 257 direction of the thermal wind shear (i.e. down-front,  $EBF > 0$ ) will drive a frictional Ekman

258 transport that forces dense water over light, acting to steepen the front and reduce the vertical  
 259 stratification (Thomas and Lee, 2005), injecting positive PV (in the southern hemisphere) into  
 260 the ocean, encouraging  $fq < 0$ . The interaction of wind stress with the relative vorticity of the  
 261 ocean front can also induce Ekman convergence/divergence, and drive vertical motions (Thomas  
 262 and Lee, 2005). Thus, independent of any air-sea heat and salt fluxes, down-front winds are  
 263 destabilizing. For comparison with previous studies, we convert EBF into an equivalent heat flux  
 264 (e.g. Thompson et al., 2016):

$$265 \quad Q_{EK} = -\frac{\rho_0 C_p}{\alpha g} EBF \quad [11]$$

266 where  $C_p$  is the specific heat of seawater (taken here as  $3992 \text{ J kg}^{-1} \text{ }^\circ\text{C}^{-1}$ ), and  $\alpha$  is the thermal  
 267 expansion coefficient, a function of salinity and temperature.  $EBF$  used here is calculated using  
 268 the 2 m density gradient derived from the underway measurements. A negative  $Q_{EK}$  (associated  
 269 with down-front winds,  $EBF > 0$ ) destabilizes the mixed layer.

270 The total air-sea heat flux is  $Q_{HF} = Q_{shortwave} + Q_{longwave} + Q_{latent} + Q_{sensible} + Q_{rain}$  ( $\text{W m}^{-2}$ ).  $Q_{HF}$  is  
 271 calculated from shipboard meteorological and oceanographic observations using the COARE  
 272 3.0a bulk algorithms (Fairall et al., 1996). When  $Q_{HF}$  is positive (negative), the ocean gains  
 273 (loses) heat, stabilizing (destabilizing) the water column.

#### 274 **iv. Frontogenesis**

275 The frontogenesis function provides a measure of the rate at which horizontal velocity gradients  
 276 can increase the lateral buoyancy gradient (Hoskins, 1982),

$$277 \quad F = 2 \left( -\frac{\partial u}{\partial x} \frac{\partial b}{\partial x} \right) \frac{\partial b}{\partial x} \quad [12]$$

278  $F$  is one term in the equation for the Lagrangian evolution of the horizontal buoyancy gradient  
 279 (Holmes et al., 2014),  $\frac{D}{Dt} \left| \frac{\partial b}{\partial x} \right|^2$ , and is calculated using the Triaxus-measured buoyancy gradient

280 and ADCP-measured velocity (Thomas et al., 2013).  $F > 0$  indicates that horizontal strain is acting  
281 to drive frontogenesis. Typically, this will induce an ageostrophic secondary circulation that  
282 partially balances the frontogenetic tendency (through differential vertical advection; Hoskins,  
283 1982).

#### 284 **d. Data Processing**

##### 285 *i. Co-locating in situ datasets*

286 To calculate specific terms (see §2c), the hydrographic and velocity observations need to be co-  
287 located. ADCP-measured velocity and its vertical/horizontal shear is linearly interpolated from  
288 its native grid to the Triaxus grid in  $x/z$  coordinates. The final dataset has a resolution of 1 m in  
289 the vertical and ~1 km along-track. We also tested interpolating from the Triaxus to ADCP grid,  
290 with the same results. Horizontal and vertical gradients in all properties are computed via central  
291 differencing.

##### 292 *ii. Calculating error bars*

293 To evaluate the significance of the PV field, given the limited observations available, we run a  
294 Monte Carlo experiment using error estimates of velocity ( $5 \text{ cm s}^{-1}$ ), temperature ( $0.002^\circ\text{C}$ ) and  
295 salinity (0.005 PSU). These estimates are twice the manufacturer-supplied accuracy for  
296 temperature and salinity, and twice the error found in an empirical study of the RDI S-ADCP  
297 accuracy (Fischer et al., 2003). We assume Gaussian error distributions with zero mean and STD  
298 equal to the estimated error, then randomly assign these errors to each grid point. From these  
299 new noisy fields, we calculate gradients and the terms described in §2c; then repeat one thousand  
300 times. From these one thousand realizations, we derive confidence intervals based on the  
301 Student's t-distribution, assuming a sample STD (unknown population STD), with  $N-1$  degrees  
302 of freedom.

## 303 **4. Mesoscale eddy field (austral winter 2017)**

### 304 **a. EAC eddy shedding event**

305 During August and September 2017, satellite ADT maps reveal an EAC anticyclonic eddy  
306 shedding and re-attachment event at approximately 34° S (Fig. 2). The anticyclonic eddy  
307 shedding was associated with an offshore cyclonic eddy that propagated westward. As the  
308 anticyclonic eddy detached from the EAC jet (Aug 1<sup>st</sup>-10<sup>th</sup>), the cyclonic eddy squeezed in  
309 between the two warm water masses, thus forming an eddy dipole with the anticyclone,  
310 southwest of the EAC jet separation (see Malan et al. (2020) for details on the eddy-driven cross-  
311 shelf transport of this dipole). Over this period the anticyclonic eddy slowly decayed, with  
312 decreasing ADT amplitude and spatial scale. The cyclonic eddy also shrunk as it moved  
313 westward and became constrained between the EAC and anticyclonic eddy. Toward the end of  
314 September, the cyclonic eddy was squeezed out to the south as the anticyclonic eddy reconnected  
315 with the EAC jet (Fig. 's 2 and 3).

### 316 **b. Mesoscale frontal structure**

317 The evolution of the eddy dipole generated strong fronts that divided the distinct water masses of  
318 the warm EAC, cold cyclonic eddy, and warm anticyclonic eddy (Fig. 3a). The fronts exhibit  
319 large gradients in SST over short distances (with a negative gradient within the eddy dipole ~34-  
320 35°S; Fig. 3b). The time-latitude Hovmoller plot of FSLE (Fig. 3c) shows the evolution over a 2-  
321 month period. FSLEs reach values of up to 1 day<sup>-1</sup>, characteristic of an intense strain field and  
322 similar to values found in the ACC (Siegelman et al., 2019). As the cyclonic eddy moved  
323 westward between the EAC and the anticyclonic eddy, strain increased, and FSLE values  
324 between the two eddies were intensifying as the ship passes the front. This indicates the front is  
325 undergoing frontogenesis.

326 High-resolution SST imagery of the front on the day of sampling shows it to have slight  
327 anticyclonic curvature (Fig. 4a,b). To calculate the radius of curvature  $R$ , we best fit a circle to  
328 this frontal region, obtaining  $R = 80$  km. The cyclogeostrophic Rossby number,  $C = \frac{v_\theta}{fR}$ , provides  
329 a metric of the influence of curvature on the flow (Shakespeare, 2016). Based on a depth-  
330 averaged  $v_\theta$  at the front, and the  $R$  calculated above, we obtain  $C = -0.14$ , which is relatively low  
331 and indicates a weak influence. The negative value is due to anticyclonic curvature, and implies  
332 an increase in  $v_\theta$  for the forces to remain in balance (horizontal pressure gradient, Coriolis, and  
333 centripetal).

334 At the time of in-situ sampling, the ADT-derived geostrophic speed of the onshore jet of the  
335 dipole reached a maximum of  $1.3 \text{ m s}^{-1}$  (Fig. 4f). The geostrophic vorticity (normalized by  $|f|$ )  
336 measured nearest the front reached  $-0.15 f$ , while the anticyclonic vorticity was  $0.08 f$ . Within the  
337 eddy cores, vorticity values peaked at  $-0.4 f$  and  $0.3 f$ , respectively, indicating relatively high  
338 mesoscale Rossby numbers. Even though these geostrophic measurements reveal an energetic  
339 mesoscale field, the in-situ observations presented next reveal much larger values of velocity and  
340 its spatial gradients at the submesoscale range.

## 341 **5. Submesoscale processes at the front**

### 342 **a. Submesoscale frontal structure**

343 In-situ measurements augment the large-scale view of the eddy dipole from satellite ADT  
344 observations, revealing submesoscale characteristics embedded within the mesoscale field (e.g.  
345 Fig. 4g). At the shallowest ADCP bin (centered at 28 m), the velocity of the jet core is  $1.85 \text{ m s}^{-1}$ ,  
346 with asymmetric lateral shear across the front. The cyclonic shear on the cold eastern side of the  
347 jet, measured as  $dv/dx$ , has a maximum of  $2.3f$ . Conversely, the anticyclonic shear flank of the

348 jet peaks at  $-0.76f$ , as it is constrained from exceeding  $f$  (Scherbina et al., 2013; Thomas et al.,  
349 2008). In contrast, the satellite-derived vorticity reaches a peak magnitude of  $0.4f$ . The  
350 difference between satellite-measured geostrophic and in-situ velocities reveals that while the  
351 satellite observations do a good job of representing the mesoscale, fine-scale structure at the  
352 front is not captured by altimetry.

353         Based on a high-resolution vertical slice from the Triaxus, the front has a width of  $\sim 15$   
354 km, and extends down to 200 m depth (Fig. 5). The mixed layer base ascends from  $\sim 275$  m to  
355  $\sim 175$  m over a range of 60 km. The front is demarcated by exceptionally strong horizontal  
356 gradients in all measured properties, with warmer, saltier, low-oxygen content water in the  
357 deeper mixed layer of the anticyclonic eddy, and colder, fresher, high-oxygen content in the  
358 cyclonic eddy. There is a significantly higher concentration of chlorophyll-a in the cyclonic eddy  
359 (Fig. 5f). The front tilts with depth in the direction of the anticyclonic eddy. Below the isopycnal  
360 outcrop the weakly stratified, cold and fresh surface water of the cyclonic eddy appears to  
361 subduct into the pycnocline (e.g. Fig. 5c). Undulating isopycnals at the base of the mixed layer  
362 are the signatures of internal gravity waves with amplitudes as large as 50 m and wavelengths  
363  $\sim 15$  km (if observations can be assumed near-instantaneous with respect to the propagating  
364 internal waves), and their impact is seen on all variables, particularly chlorophyll-a and oxygen  
365 (Fig. 5c,f). Without additional information it is not clear whether these waves were generated  
366 remotely or by the front itself (e.g. Shakespeare and Taylor, 2013).

367         The S-ADCP vertical profiles of the horizontal currents reveal the outcropping isopycnals  
368 are associated with strong along-front velocity, greater than  $1 \text{ m s}^{-1}$  all the way down to the base  
369 of the mixed layer (Fig. 6a). This velocity has significant vertical shear (Fig. 6c,f), and is



370 primarily in thermal wind balance along the front until the base of the mixed layer, as shown in  
371 Fig. 7b, where the departure from thermal wind balance is shown (in %) (Holmes et al., 2014):

$$372 \quad \gamma_{TWB} = \frac{\left| \frac{dv}{dz} - \frac{dv_g}{dz} \right|}{\left| \frac{dv}{dz} \right| + \left| \frac{dv_g}{dz} \right|} \times 100. \quad [13]$$

373 Outside of the narrow front, the weaker shear is predominantly ageostrophic with large  $\gamma_{TWB}$ .  
374 Such differences are expected in the mixed layer and pycnocline where internal waves are  
375 evident, but not the ageostrophic shear at the base of the front at 250 m depth, 40 km along-track  
376 (Fig. 6f); in the same region the across-front velocity is large ( $\sim 25 \text{ cm s}^{-1}$ ) and indicates the water  
377 moving in the direction of the warm core eddy (Fig. 6b). The relative vorticity is asymmetric and  
378 dominated by the cyclonic component along the front, and coincident with high strain values,  
379 typical of submesoscale motions (Fig. 6d,e) (Mahadevan, 2016).

380 The magnitude of horizontal buoyancy gradient ( $M^2$ ) at the front is  $\sim 6 \times 10^{-7} \text{ s}^{-2}$  (Fig.  
381 5e). This is very high, and comparable to strong fronts measured elsewhere (in the ACC, Adams  
382 et al., 2017; in the Kuroshio, D'Asaro et al., 2011). From 4 months of glider measurements in the  
383 ACC, Viglione et al. (2018) found  $M^2$  magnitudes exceeded  $6 \times 10^{-7} \text{ s}^{-2}$  less than 1% of the time  
384 (although this estimate is conservative given their 5 km sampling resolution and assuming the  
385 glider rarely sampled exactly perpendicular to fronts). When we calculate  $M^2$  at 2 m depth using  
386 thermosalinograph measurements with a 5 min sampling rate and a mean spatial resolution of 1  
387 km, we obtain an even greater value of  $1 \times 10^{-6} \text{ s}^{-2}$  (Fig. 5e).

388 The frontogenesis function has values of  $2.5 \times 10^{-17} \text{ s}^{-5}$  (Fig. 7a), coincident with the  
389 altimetry-derived strain rate increase at this time (Fig. 3c). Note in our calculation we use the full  
390 velocity rather than the geostrophic component, which may include strain from other sources,  
391 such as internal waves. However, similar values can be obtained by taking the ADT-derived

392 geostrophic strain ( $\sim 0.4f$ ) and average  $M^2$  at the front ( $\sim 5 \times 10^{-7} \text{ s}^{-2}$ ), giving  $F = 1.7 \times 10^{-17} \text{ s}^{-5}$ .  
393 This indicates horizontal strain is acting to increase the horizontal density gradient of the front,  
394 reaching a similar magnitude to that observed at a Gulf Stream front in Thomas et al. (2013).  
395 Fluid parcels being carried along the front in the confluent region must accelerate to remain in  
396 cross-frontal geostrophic balance. According to the semi-geostrophic momentum balance such  
397 an acceleration is balanced by an ageostrophic secondary circulation (ASC, Hoskins, 1982). This  
398 ageostrophic flow will tend to subduct water below the front from the cold cyclonic side (e.g.,  
399 see Figure 12 of Pollard and Regier, 1992). At the base of the front, there is a region of  
400 frontolysis in proximity to the subducting water parcel, associated with slightly divergent flow.  
401 This process has been noted by Holmes et al. (2014) near the Equator – convergence of water  
402 at an upper ocean front drives subduction of water, which feeds divergent flow at depth that can  
403 lead to frontolysis (although along-front convergence/divergence can also absorb this subducting  
404 flow).

## 405 **b. Subduction**

406 Subduction of water appears to be occurring at 200 m depth, 55 km along-track (Fig. 5-8). This  
407 is a region of anticyclonic vorticity (Fig. 6d), which leads to near-zero absolute vorticity (defined  
408 here as  $\zeta_a = f + \partial v / \partial x$ ) in this water parcel as  $f \approx -8 \times 10^{-5} \text{ s}^{-1}$ . This water parcel also  
409 exhibits low stratification, low-magnitude PV (Fig. 7c), and is associated with high oxygen and  
410 chlorophyll-a content (Fig. 5c,f). The low magnitude PV water parcel is separated from the  
411 mixed layer by a band of negative PV (i.e. white parcel in Fig. 7c). This is characteristic of the  
412 formation mechanism of ITEs, as shown in the simulations of Spall (1995) and Thomas, (2008).  
413 Their simulations show that ITEs can evolve from subducted water, which separates from the  
414 mixed layer and moves into the thermocline, with anticyclonic vorticity, low-magnitude PV and

415 water properties of the mixed layer (i.e. high oxygen, low stratification, and T/S anomalies to the  
416 ambient thermocline water). The water parcel we observe has the same properties as the cyclonic  
417 eddy mixed layer, but with the opposite sign of vorticity; from this we can infer that the parcel  
418 gained anticyclonic vorticity as it subducted (Fig. 6d). If PV is conserved, then the generation of  
419 anticyclonic vorticity can occur via vortex squashing (Spall, 1995), or by differential vertical  
420 motions that drive vortex tilting of the horizontal vorticity associated with the along-front  
421 vertical shear (Thomas, 2008; Holmes et al., 2014). The subducting water parcel in our  
422 observations bears a striking resemblance to the model results of Thomas (2008) (their Figure 5).  
423 The generation of a coherent ITE is not guaranteed to occur for all subducting water parcels  
424 because mesoscale straining can disrupt the process by shearing apart the nascent subducting  
425 water parcel in elongated ribbons of low PV (see Thomas (2008), their Figure 4). This may be  
426 the case here, but we cannot tell from our transient viewpoint.

427         There are several mechanisms that can drive frontal subduction of surface water into the  
428 thermocline. In the idealized simulations of Spall (1995) and Thomas (2008), it is baroclinic  
429 instability of the frontal jet that drives vertical circulation. As the jet meanders and generates  
430 eddies, it generates confluent (divergent) flow associated with the downstream (upstream) side of  
431 the meander crests, that compresses (expands) the horizontal density gradient. The along-front  
432 velocity accelerates (decelerates) to remain in thermal wind balance, which is compensated for  
433 by an eddy overturning cell, leading to downwelling on the denser side and upwelling on the  
434 lighter side. However, Spall (1997) showed that when the front is subjected to a large-scale  
435 deformation field, the subduction rate is dominated by the resulting frontal ASC rather than time-  
436 dependent upwelling/downwelling associated with meandering. More recently, Brannigan et al.

437 (2017) showed in an idealized model that subduction only existed in their highest-resolution  
438 model runs (0.25 and 2 km, and not 4km), and was directly related to submesoscale instabilities.  
439 From the observations alone, we cannot state conclusively which mechanism is driving the  
440 subduction, or if different mechanisms are occurring simultaneously (Spall, 1997). However,  
441 given the large-scale strain observed, we expect that strain-induced frontogenesis and the  
442 resultant ASC plays a central role. Vertical velocity scales as  $W \sim Ro\delta U$  where  $Ro$  is the Rossby  
443 number ( $\zeta/f$ ),  $\delta$  is the ratio of depth to length scales ( $D/L$ ), and  $U$  is the characteristic velocity  
444 (Mahadevan, 2016). Based on the observations of the water parcel here,  $W \sim 250 \text{ m day}^{-1}$  (for  
445  $Ro=1$ ,  $D=50 \text{ m}$ ,  $L=15 \text{ km}$ ,  $U=1 \text{ m s}^{-1}$ ), signifying very strong vertical motions associated with  
446 the front. Based on asymmetric vorticity distribution, we would expect the vertical velocity to  
447 exhibit stronger downwelling velocities over a smaller area in the cyclonic zone, compared with  
448 broader, slower upwelling in the anticyclonic zone (Mahadevan and Tandon, 2006). Previous  
449 studies calculated the Omega equation (e.g. Rudnick, 1996), but we have not done so considering  
450 the degree of ageostrophy exhibited (Fig. 7b), and that both quasi-geostrophic (QG) and surface  
451 QG Omega equations fail to capture Rossby number  $O(1)$  submesoscale dynamics (Mahadevan,  
452 2016). In the following sections we show the presence of submesoscale instabilities that may  
453 have also played a role in this subduction.

### 454 **c. Submesoscale instability and atmospheric forcing**

455 There is a region of positive PV at the base of the front, in close proximity to the subducted  
456 parcel (Fig. 7c). Positive PV in the southern hemisphere ( $f q < 0$ ) is inherently unstable (Hoskins,  
457 1974). A zoomed-in view of the area (Fig. 8) reveals that this positive PV occurs due to a stable  
458 but weak  $N^2$ , such that  $q_{vert}$  is weak, and a strong  $M^2$ , indicating the predominance of the  
459 baroclinic PV component  $q_{bc}$  in generating  $f q < 0$  (Section 2c(ii)). We calculated PV in both

460 Cartesian and cylindrical coordinates, and found an average percent difference of 9% (we show  
461 PV calculated in cylindrical coordinates, per Equation [9], in Fig. 7 and 8). PV with the opposite  
462 sign of  $f$  due to a strong  $M^2$  and weak  $N^2$  signifies the potential for symmetric instability, as  
463 opposed to gravitational or inertial instabilities (Thomas et al., 2013). Symmetric instability, also  
464 termed slantwise convection (Taylor and Ferrari, 2009), produces a slanted overturning cell at  
465 the base of the front.

466 Positive PV can only be created by surface forcing across the isopycnal outcrop, and is  
467 ephemeral since it initiates instabilities that act to mix it out and return the flow to marginal  
468 stability. To investigate the source of positive PV observed at this front, we consider the  
469 atmospheric conditions around this time period (Fig. 4c and Supplementary Materials). The air-  
470 sea heat flux, calculated from shipboard meteorological and oceanographic measurements at the  
471 front, was destabilizing, exhibiting ocean heat loss of up to  $200 \text{ W m}^{-2}$  to the atmosphere across  
472 the front (Fig. 4c). Such heat fluxes can generate  $f q < 0$  (Haine and Marshall, 1998), and influence  
473 frontogenesis and enhance subduction (Yoshikawa et al., 2001). However, when compared to the  
474 effect of wind forcing at the front, the heat flux is an order of magnitude smaller. In Fig. 4c, the  
475 effect of wind is represented as an Ekman equivalent heat flux ( $Q_{EK}$ ). During in-situ sampling of  
476 the front, winds were upfront, with a positive  $Q_{EK}$  of  $\sim 2500 \text{ W m}^{-2}$ . Therefore, any water column  
477 destabilization via the surface heat flux would have been counteracted by the much larger  
478 stabilizing effect of wind forcing.

479 However, preceding the period of in situ sampling, the wind was down-front (between 8-10<sup>th</sup>  
480 Sep; see Supplementary Materials). Without recourse to additional observations, we can only  
481 speculate that this wind forcing may have generated the positive PV we observed on the 12<sup>th</sup> Sep,  
482 which could be a remnant of a larger region of positive PV that subsequently mixed out. The PV

483 we observed was at the base of the front, furthest from the influence of stabilizing wind. Indeed,  
484 the isopycnals at the base are more vertical, while higher in the water column they are more tilted  
485 as would be expected from upfront winds. Mahadevan (2016) note it can take several inertial  
486 periods to mix out positive PV. Our observations are taken just over 2 inertial periods after  
487 down-front winds stopped (inertial period at 35°S is ~21 hrs). Taylor and Ferrari (2009) note the  
488 existence of a ‘fossil remnant mode’ of symmetric instability of longer wavelength that persists  
489 after the most-unstable mode has mostly driven PV back to zero. We see most of the front is  
490 tilting toward re-stratification; it is only at the base where the front is still vertical, and  
491 characterized by strong  $M^2$  and weak  $N^2$ .

#### 492 **d. Baroclinic instability**

493 Satellite imagery shows the presence of cyclonic eddies along the front 2 days later, on the 14-  
494 15<sup>th</sup> Sep (Fig. 9), with length scales of ~15 km (unstable wavelength of ~30 km). The  
495 submesoscale horizontal length scale can be expressed in terms of the horizontal or vertical  
496 buoyancy gradients, as  $L = M^2 H / f^2$  or  $L = NH / f$ , respectively (Thomas et al., 2008). Using mean  
497 in-situ values of the buoyancy gradient at the front ( $M^2 = 5 \times 10^{-7} \text{ s}^{-2}$  and  $N^2 = 5 \times 10^{-5} \text{ s}^{-2}$ )  
498 and frontal depth  $H = 200 \text{ m}$  yields  $L = 14 \text{ km}$  (17 km), based on  $M^2$  ( $N^2$ ). Thus, we expect these  
499 eddies begin as submesoscale instabilities of the front, given that they evolved from a high  $Ro$   
500 (and low Richardson) flow (Thomas et al., 2008), and with a length scale on the order of the  
501 mixed layer deformation scale. On the 13<sup>th</sup> and 14<sup>th</sup> Sep, the wind was strongly down-front and  
502 therefore would have had a destabilizing influence (Supplementary Materials).

503 Baroclinic instability can occur as frontal meandering and eddy formation. Several modeling  
504 studies have shown how baroclinic instability of a front generates cyclonic frontal eddies at the  
505 surface associated with subduction of the denser water (Spall, 1995; Manucharyan and

506 Timmermans, 2013; see §5b). However, when a large-scale deformation field is present, instead  
507 of the frontal jet devolving into a field of eddies, it remains quasi-stationary, oscillating between  
508 periods of meander growth and decay as the mesoscale frontogenesis counteracts frontolysis by  
509 instabilities (Spall, 1997). This is a qualitatively similar situation to the frontal jet observed here  
510 that is quasi-stationary and coherent – at times straight (undergoing mesoscale frontogenesis),  
511 and at another time meandering (after destabilizing winds). Indeed, Figure 9 reveals the ongoing  
512 evolution of this front, which by Sep 18<sup>th</sup> has shifted and strengthened (in temperature gradient),  
513 presumably due to frontogenesis driven by the mesoscale strain field of the dipole.

## 514 **6. Discussion**

### 515 **a. A persistent mesoscale eddy dipole pattern**

516 The front was generated by strain between two counter-rotating eddies – a mesoscale eddy dipole  
517 – that formed as the anticyclonic EAC retroflection separated from the main EAC branch, and a  
518 cyclonic eddy propagated westward in between (Section 4, Fig. 2). The eddies of the dipole had  
519 distinct water characteristics, and the geostrophic strain between their cores sharpened the  
520 existing horizontal gradients (Fig. 3c). A strain field generated by co-interacting mesoscale  
521 eddies is known to generate submesoscale gradients of buoyancy (Klein and Lapeyre, 2009).  
522 This situation pre-conditioned the flow to frontogenesis, subduction and submesoscale instability  
523 (e.g. Haine and Marshall, 1998). To investigate how typical the eddy dipole structure is, we  
524 surveyed 25 years of satellite imagery in the region. We calculate the SST gradient along a  
525 transect that bisects the dipole ( $\partial SST/\partial y$ , where  $y$  is the along-transect distance, see Fig. 10).  
526 The SST gradient emphasizes the location of fronts between warm and cold water masses, and  
527 can be used as a proxy to detect horizontal density gradients. Such mesoscale density gradients  
528 have been shown in a high-resolution model to be highly correlated with submesoscale vertical

529 velocity (Rosso et al., 2015). An eddy dipole will produce an alternating positive-negative  
530 pattern in  $\partial SST / \partial y$ . Poleward propagating dipoles are evident in a time-latitude Hovmoller plot,  
531 characterized by downward slopes of alternating positive-negative bands (Fig. 10a). There is also  
532 a clear distinction of flow characteristics upstream and downstream of the mean EAC separation.  
533 Poleward of approximately 33°S, there is significantly higher variance due to the larger eddy  
534 magnitudes, associated with ‘eddy avenue’ (Everett et al., 2012), and the characteristic positive-  
535 negative banding from eddy dipoles. The horizontal gradient of SST is correlated with the FSLE  
536 field (Fig. 10c-e), which we use to diagnose the time-integrated effect of mesoscale strain, and is  
537 associated with large buoyancy gradients (e.g. Siegelman et al., 2019). For the dipole we  
538 sampled, the SST gradient and FSLE field correlate along the transect ( $r=0.75$ ), as both metrics  
539 exhibit extrema at the frontal locations between the EAC and dipole eddies. Along-transect  
540 correlation over the 25 years of satellite imagery exhibits an event-type pattern, with short  
541 periods (days to weeks) of high correlation between the two fields when strong fronts are present  
542 in the region.

543 The persistence of fronts in this region invokes a pattern of recurrent competition between  
544 the destabilizing influence of mesoscale straining – which increases available potential energy –  
545 and the stabilizing re-stratification that occurs through rapid frontogenesis and atmospheric  
546 buoyancy fluxes that drive instabilities. Such competing forces lead to periods of frontal  
547 meandering and submesoscale instability, and periods when the front is straighter (e.g. Fig. 9)  
548 (Spall, 1997).

#### 549 **b. Submesoscale lenses of anomalous water in the Tasman Sea**

550 Results presented here may explain the generation mechanism of anomalous submesoscale  
551 lenses previously observed in the Tasman Sea (BR12) (Fig. 11). Brannigan et al. (2017)



552 hypothesized that the lenses observed by BR12 were formed by submesoscale instabilities at the  
553 surface. We present direct measurements of submesoscale features along an ocean front that lead  
554 to the subduction of surface water into the thermocline of an anticyclonic eddy. BR12 highlight  
555 that all observed lenses were within anticyclonic eddies. This agrees with the intrathermocline  
556 eddy generation mechanism; at a front between a warm and cold core eddy, the colder, denser  
557 water subducts beneath the relatively lighter anticyclonic eddy. The lifespan of these dipoles is  
558 on the order of weeks to months, so the potential for atmospheric forced frontal instabilities and  
559 subduction is high.

560         During the same cruise we observed an anomalous water lens at 600 m depth in the  
561 anticyclonic eddy, revealed by CTD measurements of oxygen, temperature and salinity  
562 (Supplementary Material). The lens had higher oxygen content than ambient water, and higher  
563 salinity and temperature. While it is difficult to discern its size based on 7 scattered CTD casts, it  
564 was not large enough to be sampled by all – only 3 sampled the feature – so it probably has a  
565 horizontal scale less than 50 km, and vertical scale of ~200 m. This closely matches the BR12  
566 lenses of ~40 km and ~200 m.

567         Bass Strait water (Fig. 1a) has been shown to flow northward into the Tasman Sea and  
568 move along the shelf for up to 200 km (BR12), during which time there are many opportunities  
569 for it to interact with anticyclonic eddies shed from the EAC. Shelf-deep ocean interaction of this  
570 type has been documented in the mid-Atlantic Bight; Gulf Stream anticyclonic eddies come into  
571 contact with shelf water, which instigates frontogenesis and subduction (Zhang and Partida,  
572 2018). The submesoscale lenses observed by BR12 had water properties matching Bass Strait.  
573 The cold core eddy sampled in September 2017 originated from offshore in the Tasman Sea, so  
574 was unlikely to contain Bass Strait water. Conversely, the BR12 mesoscale anticyclonic eddy

575 that contained the lens was a persistent feature close to the shelf throughout 2010, so had ample  
576 opportunity to interact with shelf water (Fig. 11).

### 577 **c. Implications**

578 In situ measurements reveal the front was susceptible to symmetric instability (SI). This has been  
579 demonstrated in other western boundary currents (e.g. in the Gulf Stream, Thomas et al. (2013);  
580 in the Kuroshio, D'Asaro et al. (2011)). Unlike mesoscale baroclinic instability, which leads to  
581 an inverse cascade of KE, SI extracts KE from the balanced ocean flow and provides a route for  
582 dissipation via small-scale turbulence. Such processes are an important link in the cascade of  
583 energy from large scales where it is input to the small-scale where it is dissipated (Molemaker et  
584 al., 2010; McWilliams, 2016). Observations presented here provide the first empirical evidence  
585 that the EAC system is likely to comprise this instability type, which could play an important  
586 role in the energy balance of the Tasman Sea ocean circulation.

587 The strong vertical velocity associated with submesoscale eddy-driven subduction has  
588 important implications for the export of biogeochemical tracers (heat, salt, carbon, dissolved  
589 gases, etc.) from the mixed layer below the pycnocline (Klein & Lapeyre, 2009; Omand et al.,  
590 2015; Mahadevan, 2016). A recent estimate of particulate organic carbon (POC) export showed  
591 that in regions of strong mesoscale eddy activity and seasonal MLD variability, up to 50% of  
592 POC export may occur through localized eddy-driven subduction (Omand et al., 2015). In the  
593 Tasman Sea, chlorophyll-a concentration is anomalously high south of the EAC (Everett et al.,  
594 2011), where mesoscale eddy dipoles energize submesoscale frontal instability and subduction  
595 (e.g. Fig. 7c). This coupling suggests submesoscale eddy-driven subduction contributes to both  
596 primary productivity and air-sea carbon dioxide exchange.

597 **d. Open questions**

598 Our analysis is restricted to one high-spatial resolution section of a 3D time-dependent process,  
599 so many questions remain. There are several mechanisms that can drive or influence the  
600 subduction of surface water, including: baroclinic instability of a frontal jet and resultant eddy  
601 overturning cell (e.g. Spall, 1995), strain-driven frontogenesis and resultant secondary circulation  
602 (e.g. Spall, 1997), and submesoscale instabilities, such as symmetric instability (Brannigan,  
603 2016). To delineate the relative influence of these processes requires more high-spatial resolution  
604 and time-dependent observations, which we do not have. Based on available observations (Fig. 3  
605 and 7a) and model evidence (Spall, 1997), it seems likely that strain-induced frontogenesis  
606 dominated, given the large strain values measured. However, different mechanisms can act  
607 simultaneously (McWilliams, 2016), and with observational evidence for mixed layer baroclinic  
608 instability (Fig. 9) and symmetric instability (Fig. 8) it is possible that each of these physical  
609 processes has an influence on the vertical exchange of water at this front. More questions  
610 generated by our observations – but which require numerical models to answer – include: what is  
611 the relationship between  $fq < 0$  and ITE formation? What is the mechanism by which an ITE  
612 formed at an upper ocean front moves down to depths of  $\sim 600$  m? How does variability in wind  
613 speed and direction effect the stability of a front in the presence of mesoscale strain and  
614 submesoscale instabilities?

615 **7. Summary**

616 In-situ measurements at a strong upper-ocean front reveal the existence of submesoscale  
617 variability embedded within the mesoscale circulation, south of the EAC separation zone. This  
618 front appeared to be undergoing strain-induced frontogenesis and was associated with subduction  
619 of surface water beneath the mixed layer. The subducting water parcel had low PV, high oxygen,

620 and anticyclonic vorticity, providing observational evidence for the formation of an  
621 intrathermocline eddy at an upper-ocean front, as predicted by idealized numerical simulations  
622 (Spall, 1995; Thomas, 2008). At the base of the front, measurements suggest the flow was  
623 susceptible to symmetric instability (with  $fq < 0$ ) due to a very large horizontal buoyancy gradient  
624 with a weak but stable vertical buoyancy gradient. We postulate that mesoscale frontogenesis  
625 pre-conditioned the flow to SI, and subsequent down-front winds destabilized the flow, injecting  
626 positive PV into the frontal outcrop. Two days after the front was sampled, cloud-free satellite  
627 imagery reveals beautiful submesoscale eddies along the front, with a length scale of  $\sim 15$  km  
628 (Fig. 9).

629         The frontal subduction of surface water observed here may explain the existence of  
630 anomalous submesoscale lenses observed by Baird and Ridgway (2012) at  $\sim 600$  m depth in the  
631 cores of several anticyclonic eddies. These lenses appear to be relatively common, since we  
632 identified a similar feature in the core of the anticyclonic eddy we sampled (Supplementary  
633 Material). Twenty-five years of satellite imagery reveals the existence of strong mesoscale strain  
634 coupled with strong temperature fronts in this region, and indicates that the conditions which led  
635 to frontal subduction observed here are a persistent feature. Our findings suggest that the  
636 energetic mesoscale eddy field south of the EAC separation zone is a hotspot for submesoscale  
637 instability and subduction, and generate questions about the relationship between submesoscale  
638 and mesoscale circulations, their space-time variability, net impact on the export of surface water  
639 into the ocean interior, and influence on biological productivity.

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641

642

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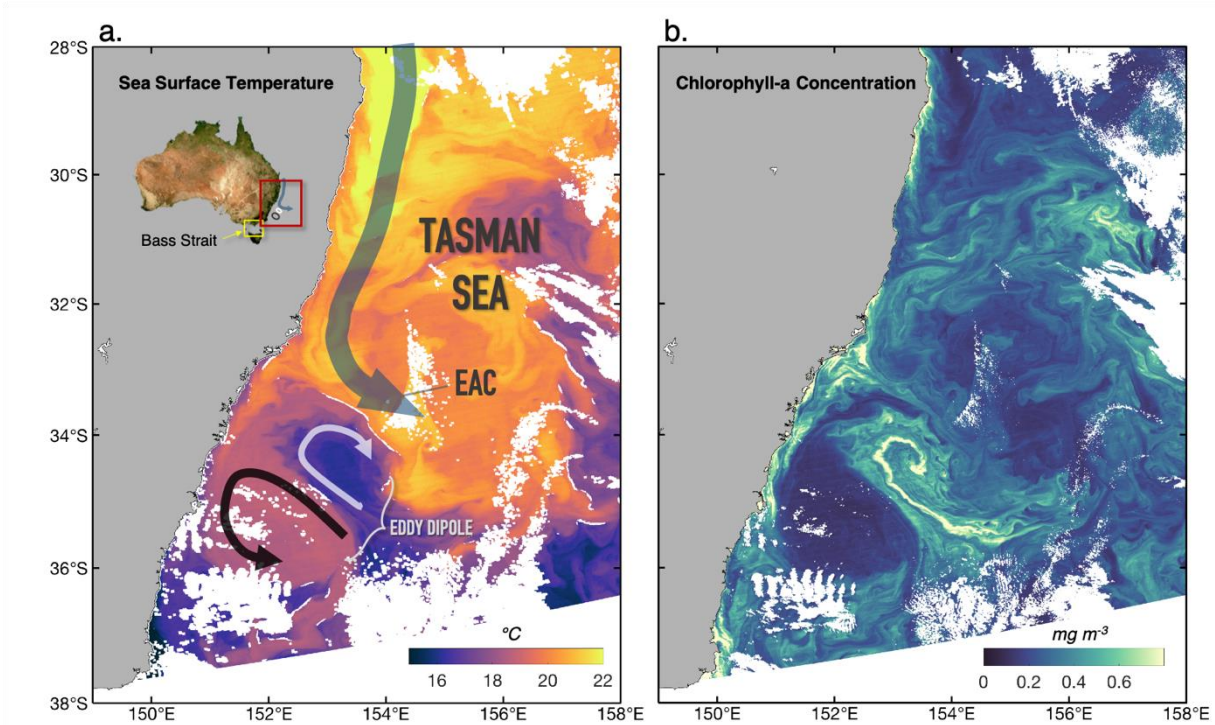
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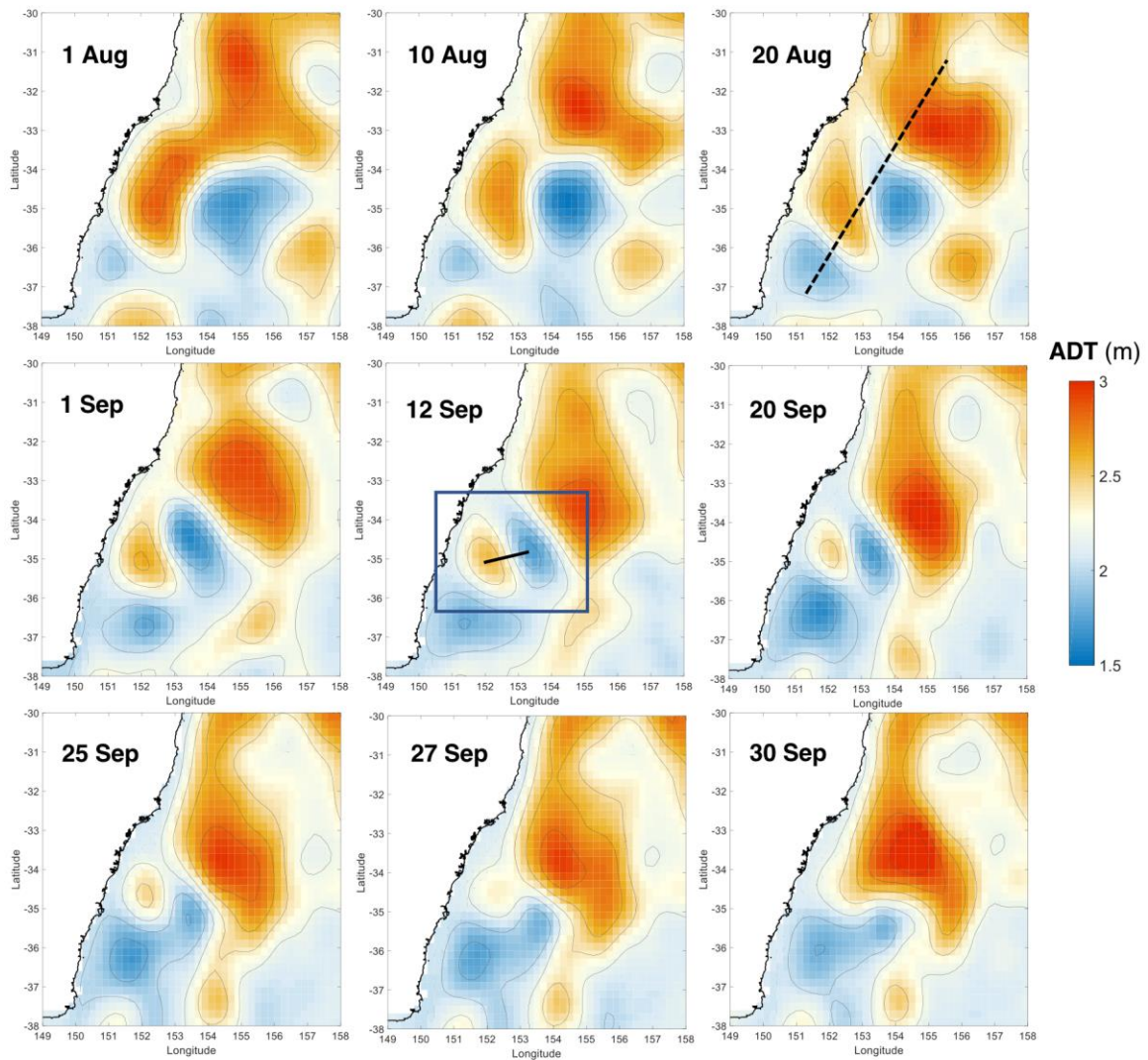
**Fig. 1** Satellite imagery in the Tasman Sea reveals the rich submesoscale tapestry of filaments and eddies present around, and within, the mesoscale eddy field; (a) Sea surface temperature ( $^{\circ}\text{C}$ ), and (b) Chlorophyll-a concentration using the OC3 algorithm ( $\text{mg m}^{-3}$ ). Both datasets are processed to level L2, with a spatial resolution of 750 m, obtained on 4 Sep 2017 from an ascending swath at approximately 3:30am Z from Suomi-NPP VIIRS. Data source: <http://oceandata.sci.gsfc.nasa.gov>. The inset figure in (a) shows the continent of Australia; the red box denotes the study area, the yellow box denotes Bass Strait, which separates Tasmania from mainland Australia. The East Australian Current (EAC) is denoted by the large gray arrow, and the eddy dipole is denoted with the white (cyclonic eddy) and black (anticyclonic eddy) arrows.

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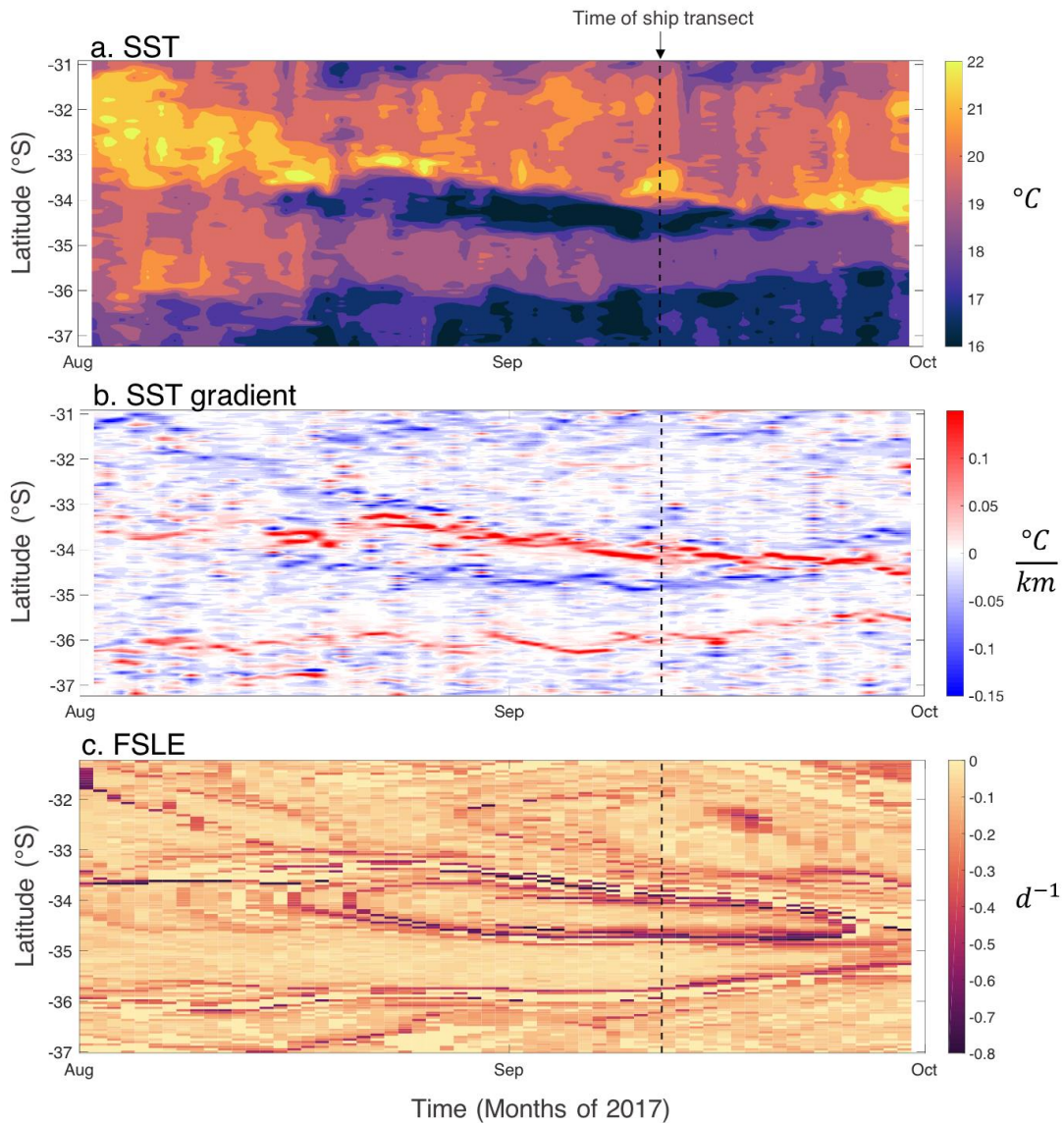
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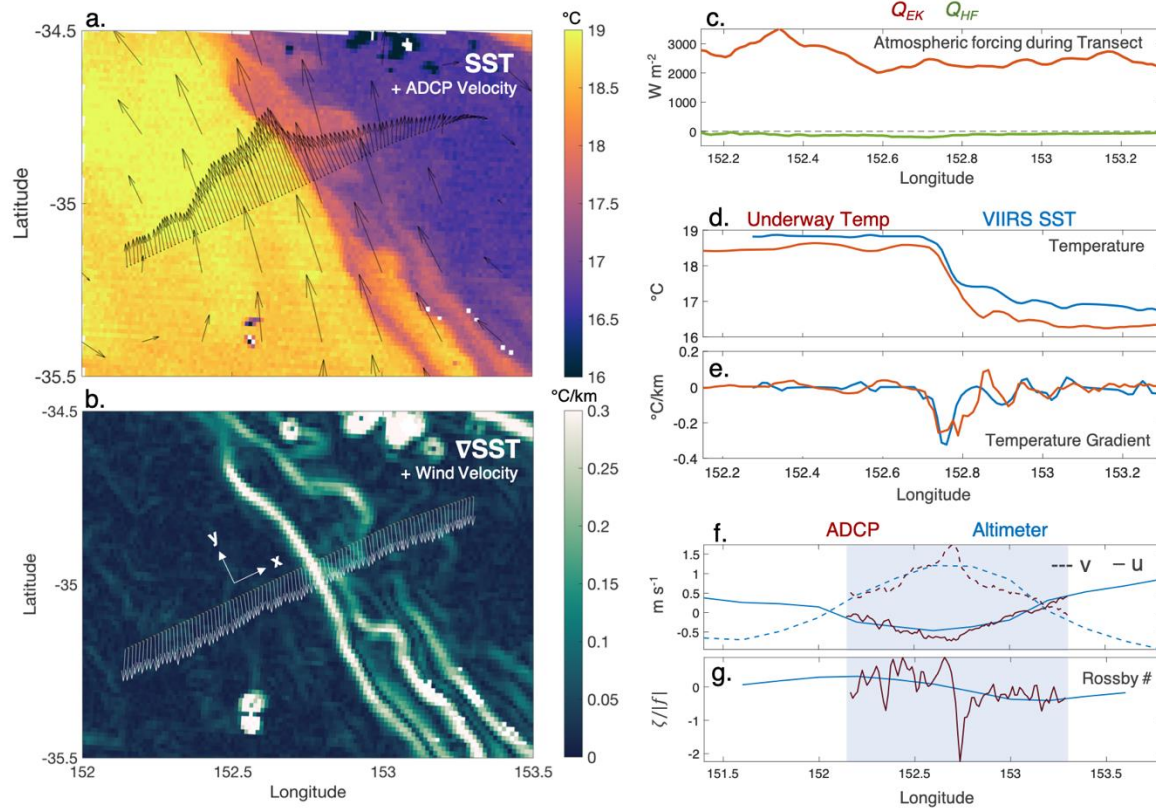
**Fig. 2** Evolution of the EAC eddy shedding event shown in 9 snapshots of absolute dynamic topography (ADT), starting August 1 when an anticyclonic eddy was shed from the EAC through to September 30, when the same feature re-attached to the EAC. On 12 September, in-situ measurements were taken along the ship transect denoted by the black line. The eddy dipole feature is encased within the blue box. The black dashed line in the top right figure denotes the transect over which the Hovmollers in Figure 3 are plotted.

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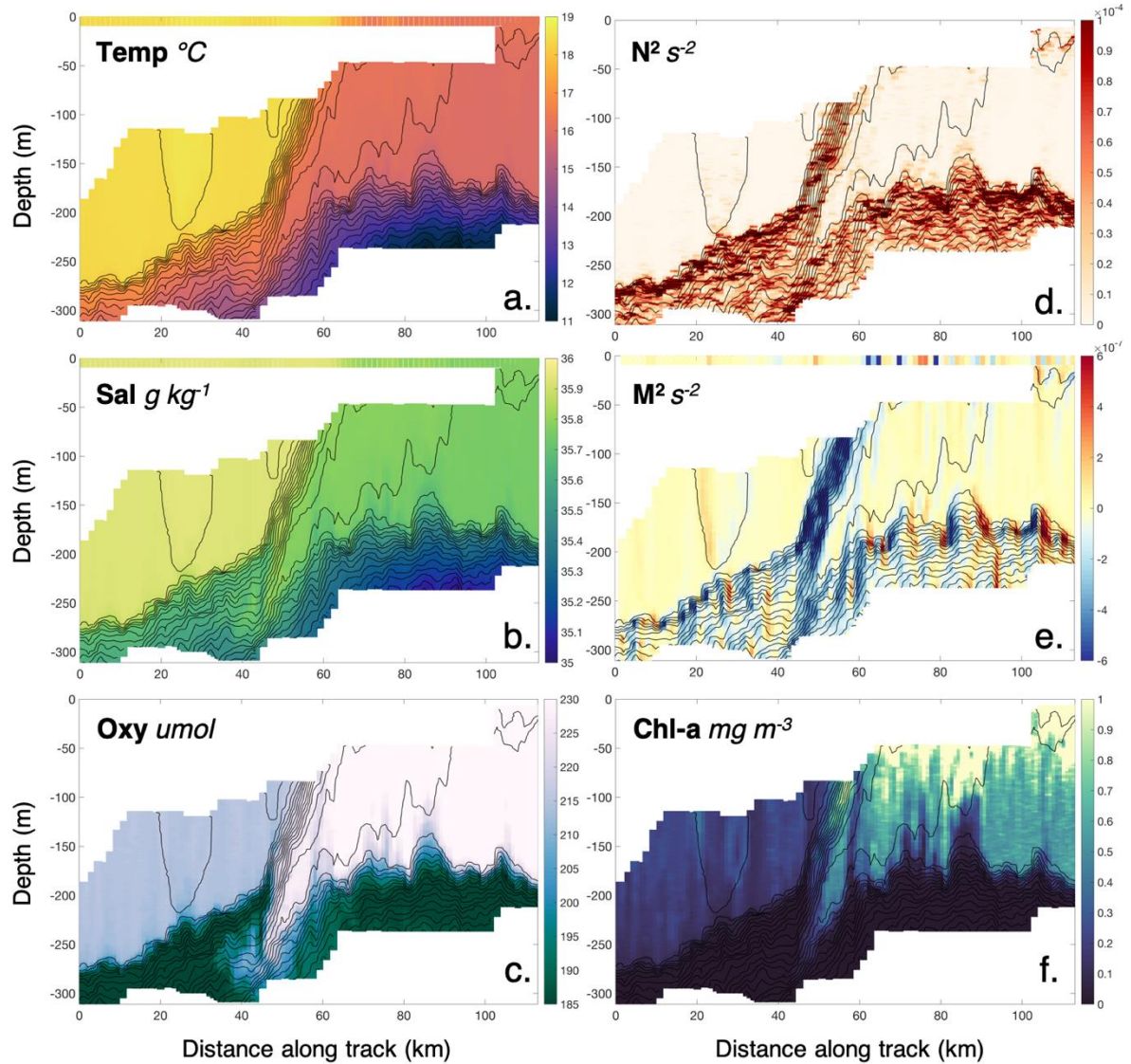


**Fig. 3** Time-latitude Hovmollers along a transect shown in Fig. 2 during August to September reveal the evolution of: (a) SST; (b) Along-transect gradient in SST, which highlights the thermal fronts between the eddies and the EAC; (c) FSLE ( $\text{day}^{-1}$ ), which characterizes the strain field over time. The black dashed line denotes the 12<sup>th</sup> of September when the in-situ measurements were taken. For consistency and time coverage, the SST used here is the objectively analyzed daily blended L4 SST 1 km resolution product (PO.DAAC g1sst product: <https://podaac-opendap.jpl.nasa.gov/>).





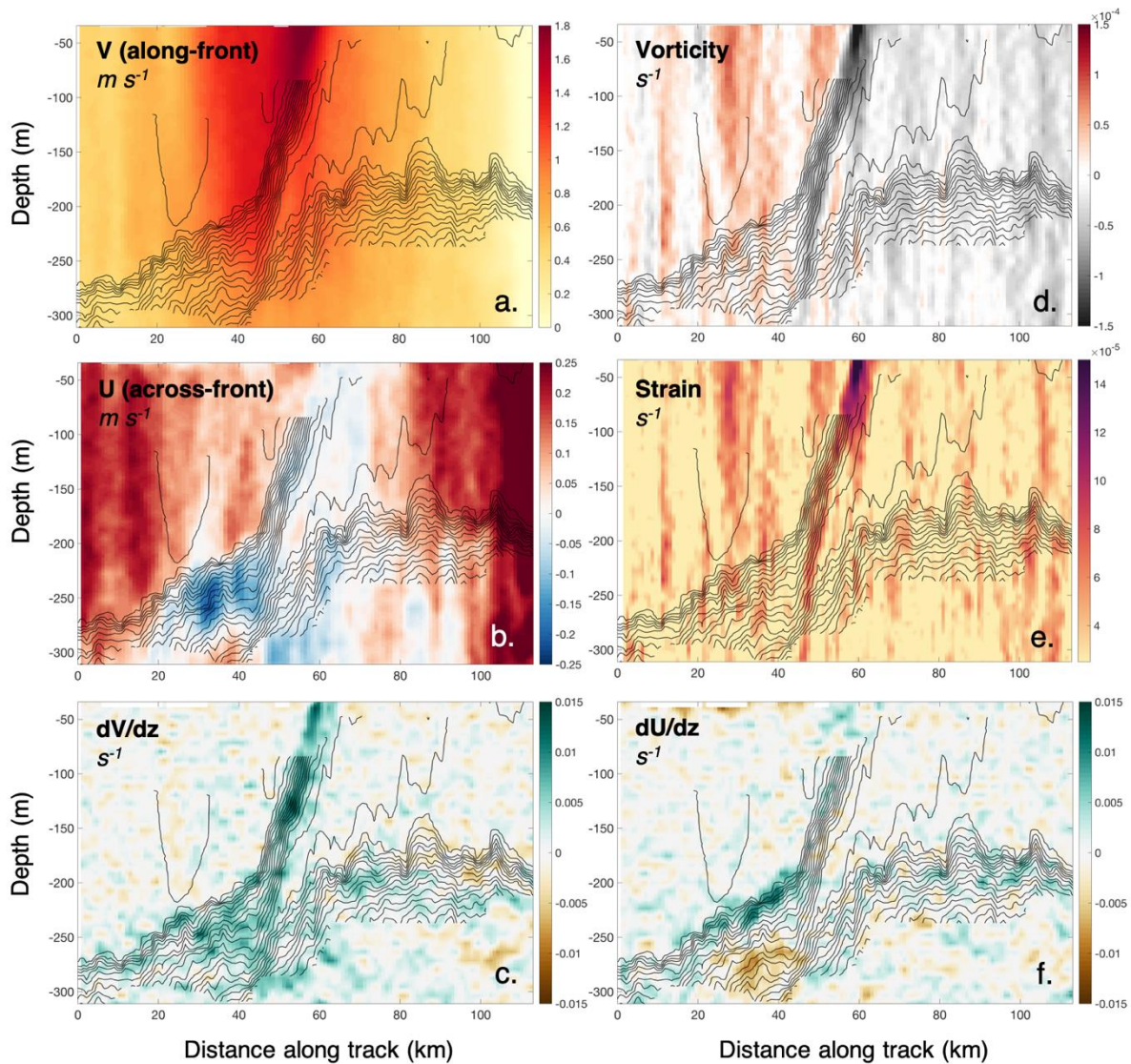
**Fig. 4** (a) A VIIRS L2 swath measurement of SST on 12 September at approx. 15:42 Z, the day the ship transected the front. The black arrows show ADCP-derived horizontal currents at 28 m; (b) The horizontal gradient of the SST field. The white arrows show shipboard-measured wind velocity, which is upfront at this time. The local Cartesian coordinates used to calculate derivatives is shown; (c) Atmospheric forcing during in situ sampling; the total heat flux  $Q_{HF}$  (negative indicates the ocean loses heat) and Ekman equivalent heat flux  $Q_{EQ}$  (positive indicates upfront winds with a stabilizing influence); (d) in situ underway temperature measurement at 2 m and the SST interpolated onto the transect; (e) the along-transect gradient of the underway temperature and VIIRS SST; (f) Meridional ( $v$ ) and zonal ( $u$ ) velocity components; and (g) relative vorticity normalized by  $|f|$ , for ADCP-derived currents (red), and ADT-derived geostrophic currents interpolated onto the transect (blue). (SST data source: <http://oceandata.sci.gsfc.nasa.gov>).



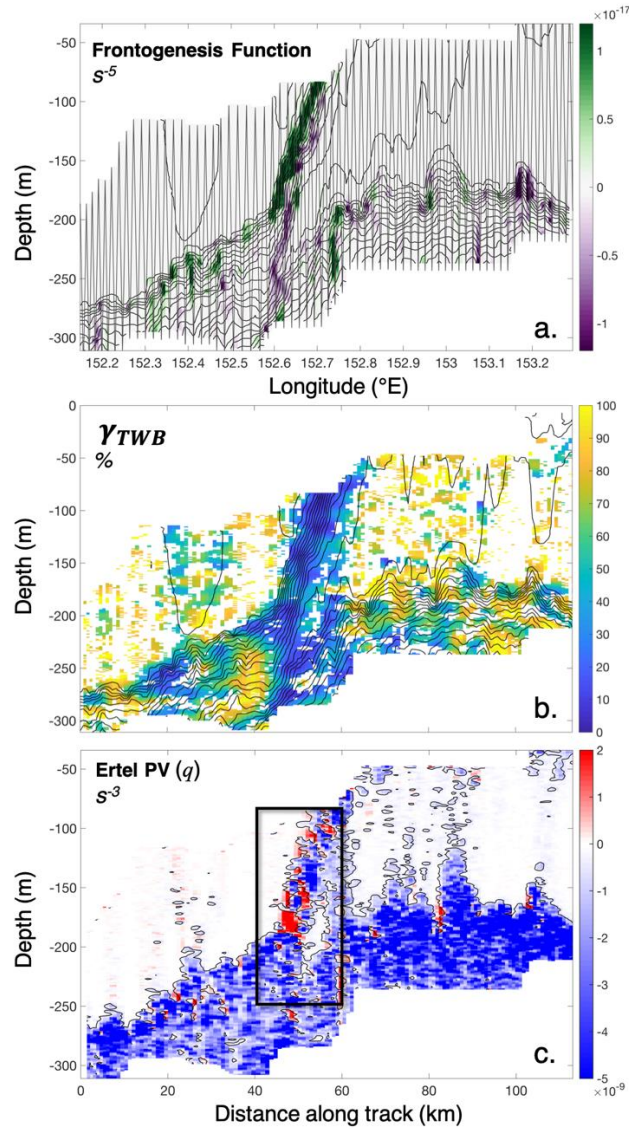
**Fig. 5** Cross-front ( $x$ - $z$  plane) sections measured by the Triaxus: (a) conservative temperature ( $^{\circ}\text{C}$ ), (b) absolute salinity ( $\text{g kg}^{-1}$ ), (c) dissolved oxygen ( $\mu\text{mol}$ ). Derived variables are: (d)  $N^2$  the Brunt-Vaisala frequency ( $\text{s}^{-2}$ ), (e)  $M^2$  the horizontal density gradient ( $\text{s}^{-2}$ ; note  $f^1 M^2$  is thermal wind balance) and (f) chlorophyll-a ( $\text{mg m}^{-3}$ , as derived from fluorescence). Line contours represent potential density referenced to the surface, from  $1025.7$  to  $1026.7 \text{ kg m}^{-3}$  in intervals of  $0.035 \text{ kg m}^{-3}$ . In panels (a,b,e), data from the underway thermosalinograph at  $2 \text{ m}$  depth has been plotted.

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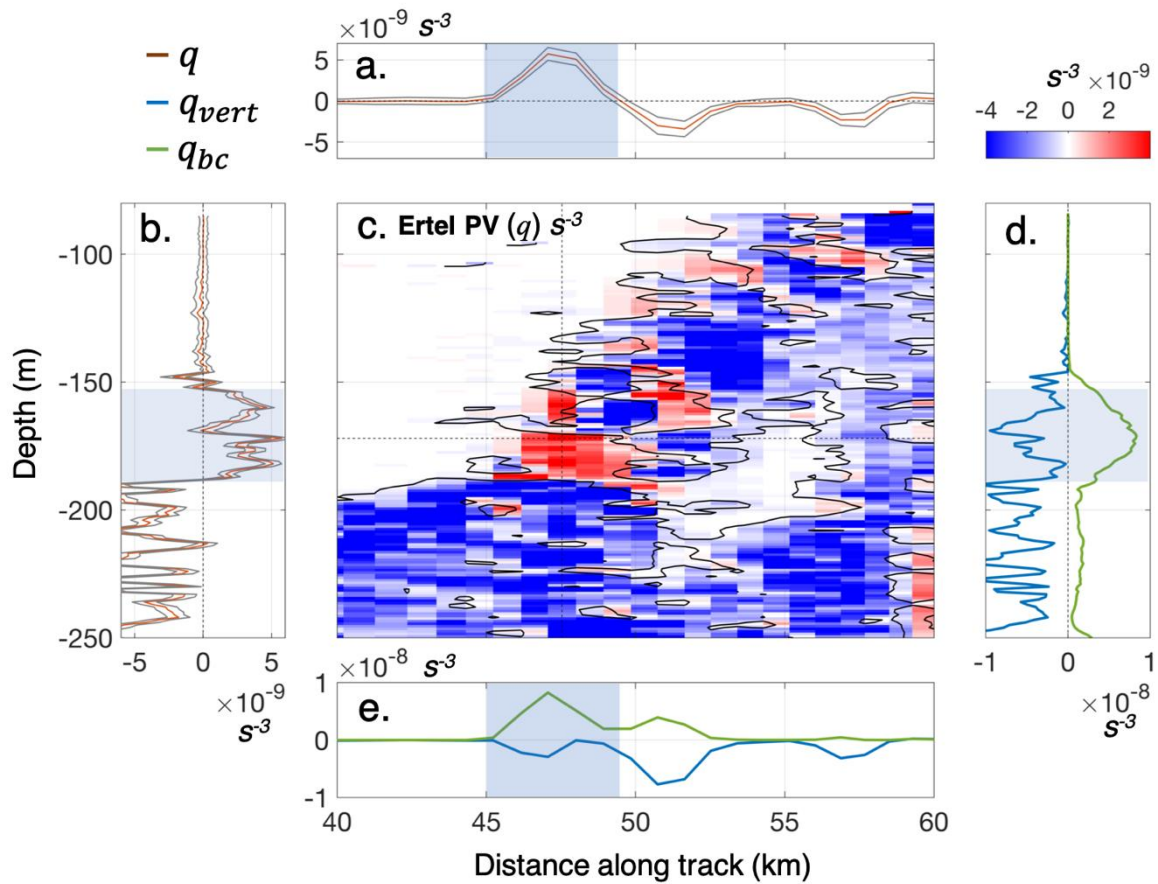
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**Fig. 6** Cross-front ( $x$ - $z$  plane) sections measured by the shipboard-ADCP: (a) along-front velocity ( $\text{m s}^{-1}$ ); (b) across-front velocity ( $\text{m s}^{-1}$ ); (c) vertical shear of along-front velocity ( $\text{s}^{-1}$ ); (d) vertical relative vorticity ( $\text{s}^{-1}$ ); (e) strain; (f) vertical shear of across-front velocity ( $\text{s}^{-1}$ ). Line contours represent potential density referenced to the surface, from  $1025.7$  to  $1026.7 \text{ kg m}^{-3}$  in intervals of  $0.035 \text{ kg m}^{-3}$ .



**Fig. 7** Cross-front ( $x$ - $z$  plane) sections of variables derived from both hydrographic and velocity measurements: (a) Frontogenesis function, superimposed in gray lines is the Triaxus profile track; (b) percent error of thermal wind balance ( $\gamma_{TWB}$ ); if the flow is in perfect thermal wind balance,  $\gamma_{TWB}$  will be zero. Cells not statistically significant have been blanked out; (c) Ertel potential vorticity ( $q$ ); In (a) and (b), line contours represent potential density referenced to the surface, from 1025.7 to 1026.7  $\text{kg m}^{-3}$  in intervals of 0.035  $\text{kg m}^{-3}$ . In (c), line contours represent the mixed layer PV =  $5 \times 10^{-10} \text{ s}^{-3}$ . The black box denotes the zoomed-in region shown in Fig. 8.



**Fig. 8** Panel (c) shows a zoom-in of Ertel PV ( $q$ ), the region denoted by the black box in Fig. 7c. Line contours represent the mixed layer PV =  $5 \times 10^{-10} \text{ s}^{-3}$ . Panels (a) and (b) show a 1-D profile of PV in distance and depth, respectively. Blue lines denote the confidence intervals. Panels (d) and (e) show 1-D profiles of  $q_{bc}$  (green line) and  $q_{vert}$  (blue line). The gray shaded bands denote the region of positive PV, which is inherently unstable.

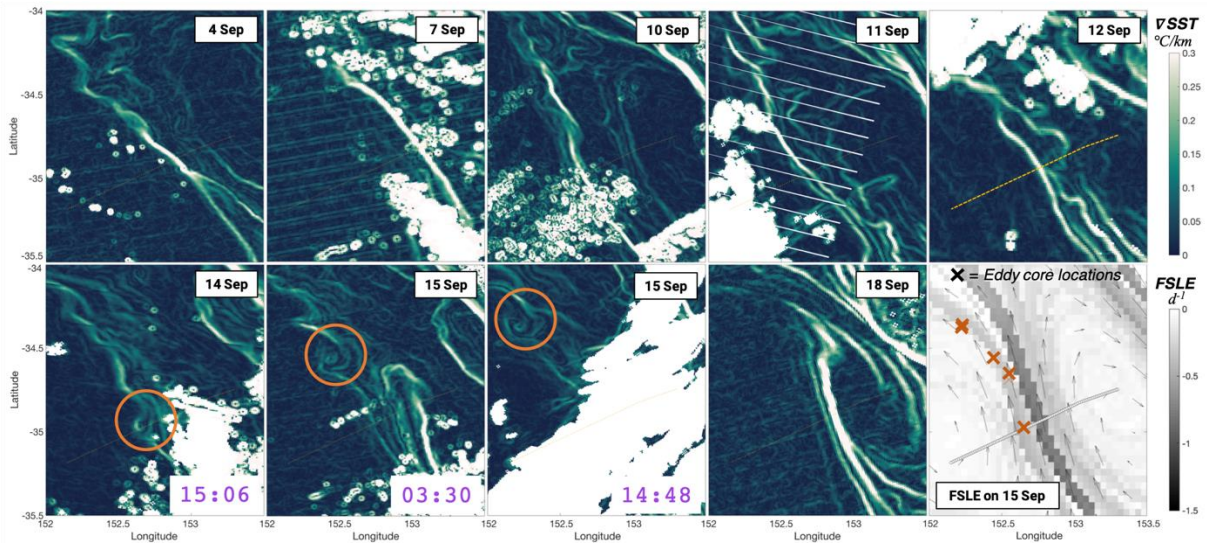
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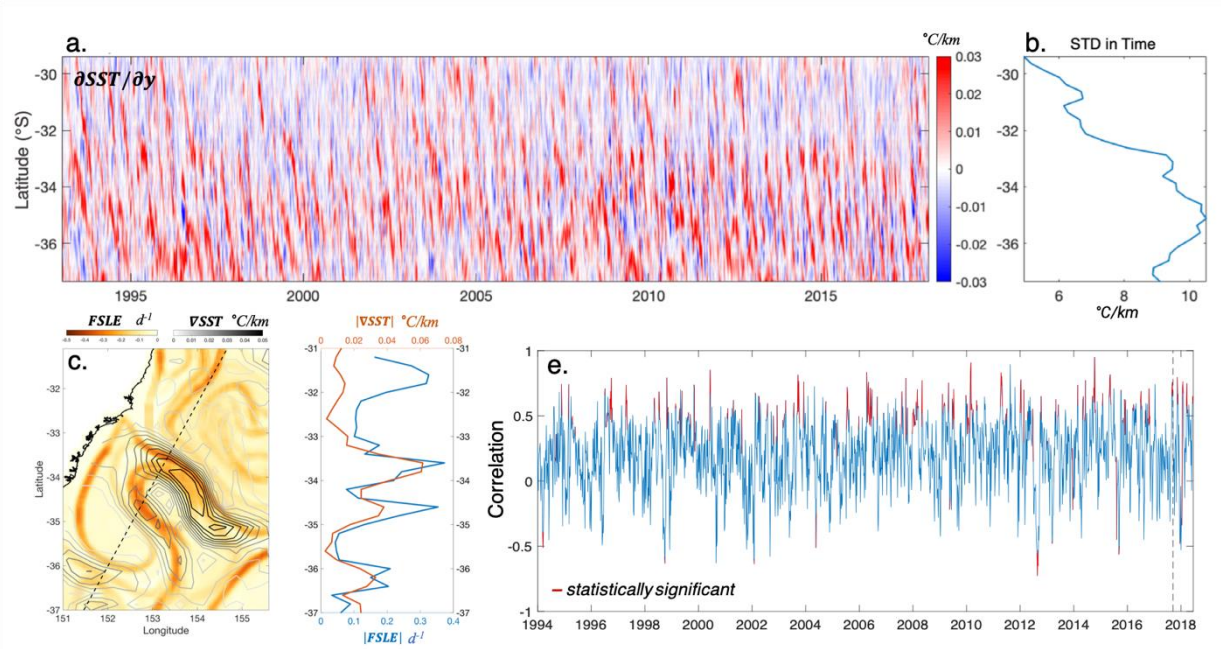


**Fig. 9** High-resolution swath measurements of SST from VIIRS. These panels show the progression of the front before, during, and after in situ sampling. Frontal instabilities are observed in satellite imagery on 12-15<sup>th</sup> Sep, with a wavelength of ~30 km. The colormap denotes the horizontal gradient in SST. The data are processed to level L2, with a spatial resolution of 750 m, obtained on 15 Sep 2017 from an ascending swath at approximately 3:30am Z from Suomi-NPP VIIRS. Data source: <http://oceandata.sci.gsfc.nasa.gov>. (bottom right) FSLE on 15<sup>th</sup> Sep shows good agreement to the high-resolution SST frontal images. Red crosses denote centers of the frontal instability highlighted by orange circles on days 14 and 15<sup>th</sup> Sep.

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**Fig. 10** (a) Satellite-derived time-latitude Hovmoller plots, and (b) time standard deviation of the mesoscale SST gradient reveals strong eddy activity poleward of  $\sim 32^\circ$  S. (c) FSLE (spatially smoothed) on 4<sup>th</sup> Sep, superimposed by contour lines of the horizontal SST gradient shows the strong match of these values at frontal zones. The black line denotes the transect over which the Hovmoller and the correlation were taken; (d) Along-transect values of  $|FSLE|$  and  $|VSST|$  as shown in (c); (e) along-transect correlation between  $|FSLE|$  and  $|VSST|$  reveals event-type distribution of periods with high correlation, when anticyclonic eddy shedding events or eddy dipoles are active in the Tasman Sea.

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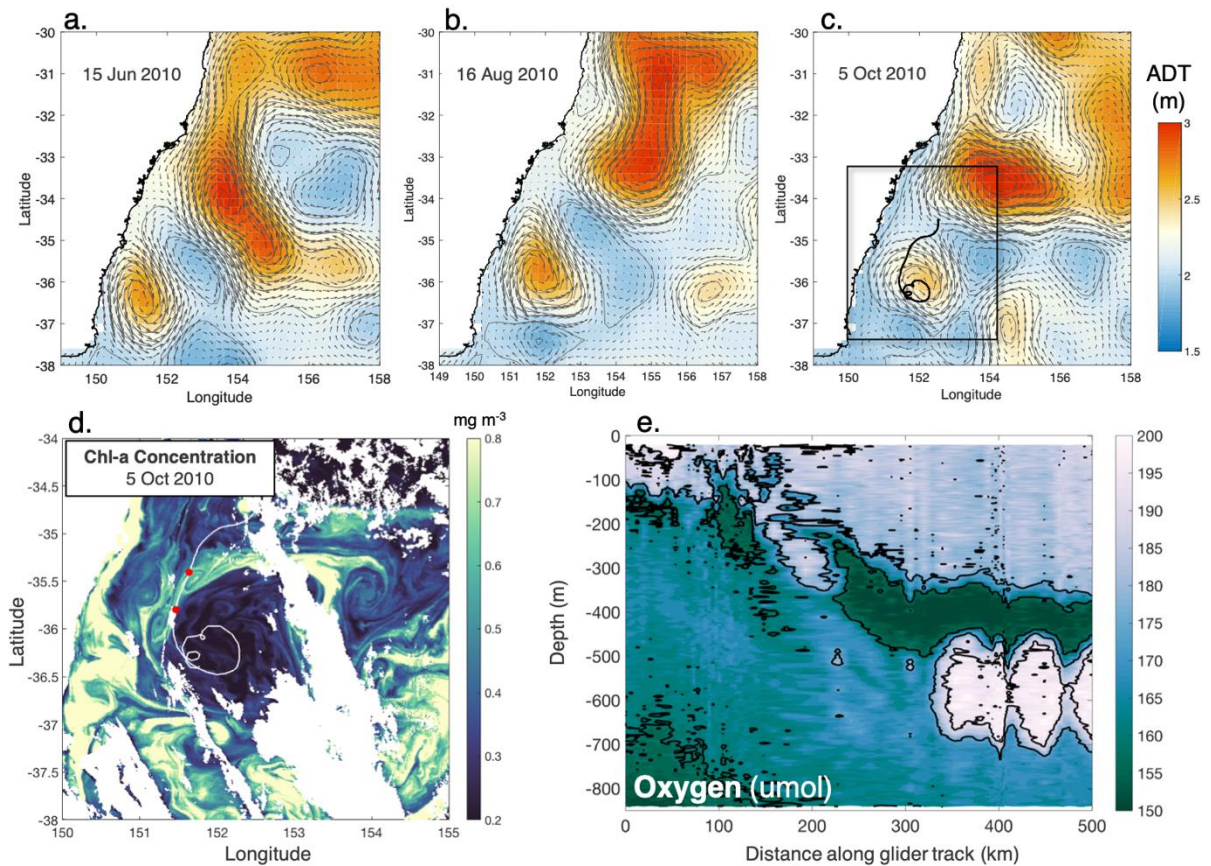
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**Fig. 11** The anomalous submesoscale lens observed by Baird and Ridgway (2012). ADT maps superimposed with geostrophic currents on (a) 15 June 2010, (b) 16 August 2010, and (c) 5 October 2010, showing the evolution and persistence of the mesoscale anticyclone. (d) Chlorophyll-a concentration from the OC3 algorithm ( $\text{mg m}^{-3}$ ), and (e) Glider measurements of oxygen along the track denoted by the black line in (c) and white line in (d). A subducting tongue of high oxygen water is evident at the periphery of the anticyclone – the glider sampling of this tongue feature is denoted by the red stop/start circles in (d).

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